

## Lecture 5

### PN Junction

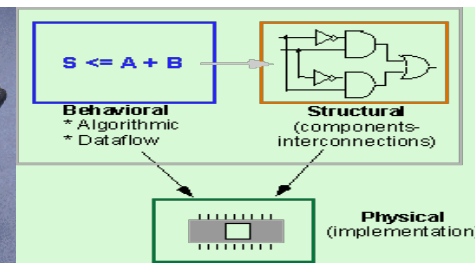
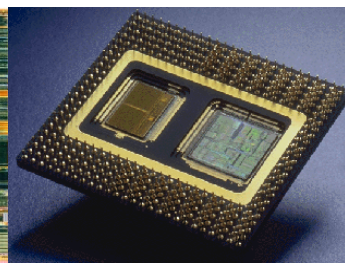
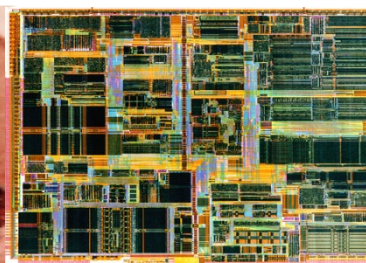
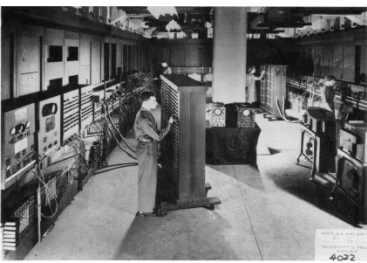
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Adapted from Modern Semiconductor Devices for Integrated Circuits, Chenming Hu, 2010

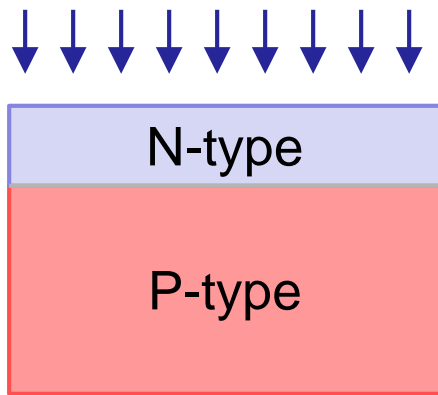


# Nature of PN Junction

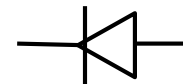
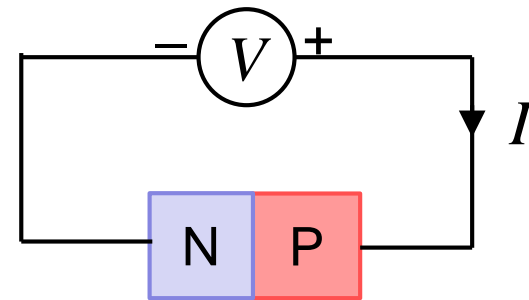
- We have considered properties of N and P-type semiconductors in isolation
- What happens when we have a transition in a single crystal from one type to the other ?

## *Fabrication*

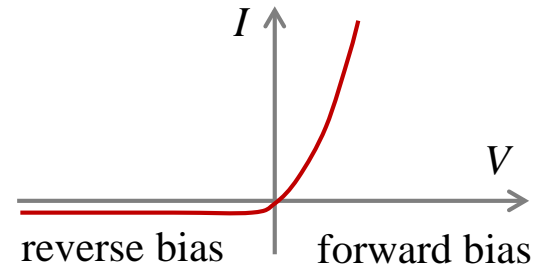
### *Donor ions*



- PN junction present in perhaps every semiconductor device

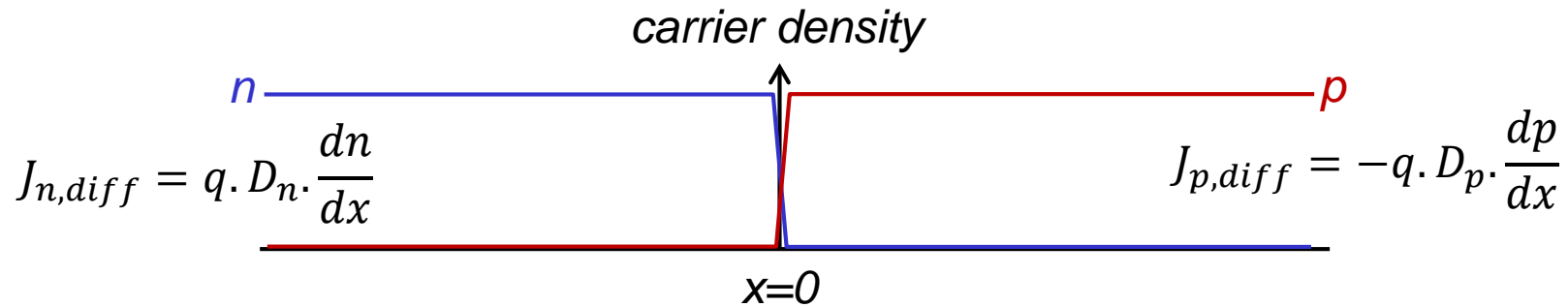
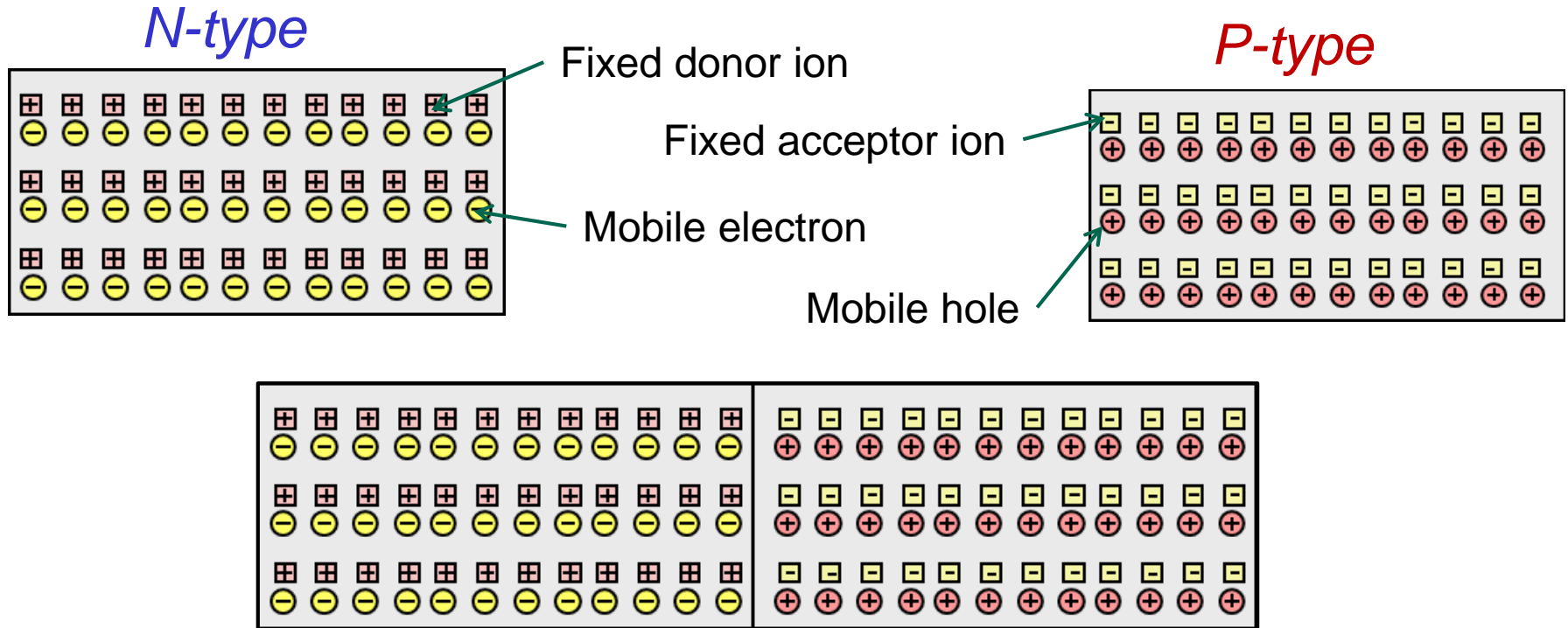


*PN  
Junction  
Diode*



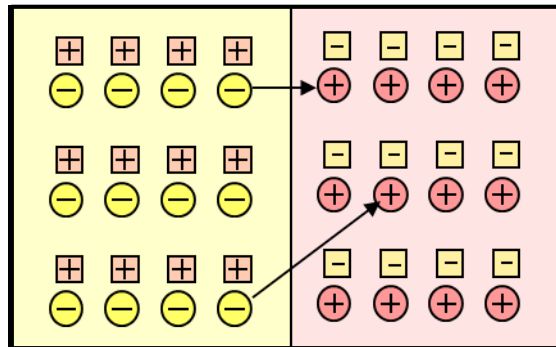
# Abrupt PN Junction

- Suppose we bring N & P crystals together:

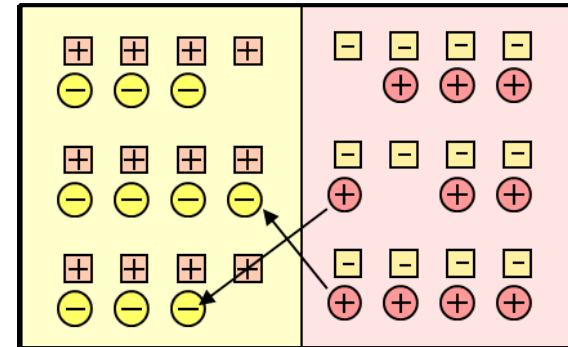


# Carrier Diffusion

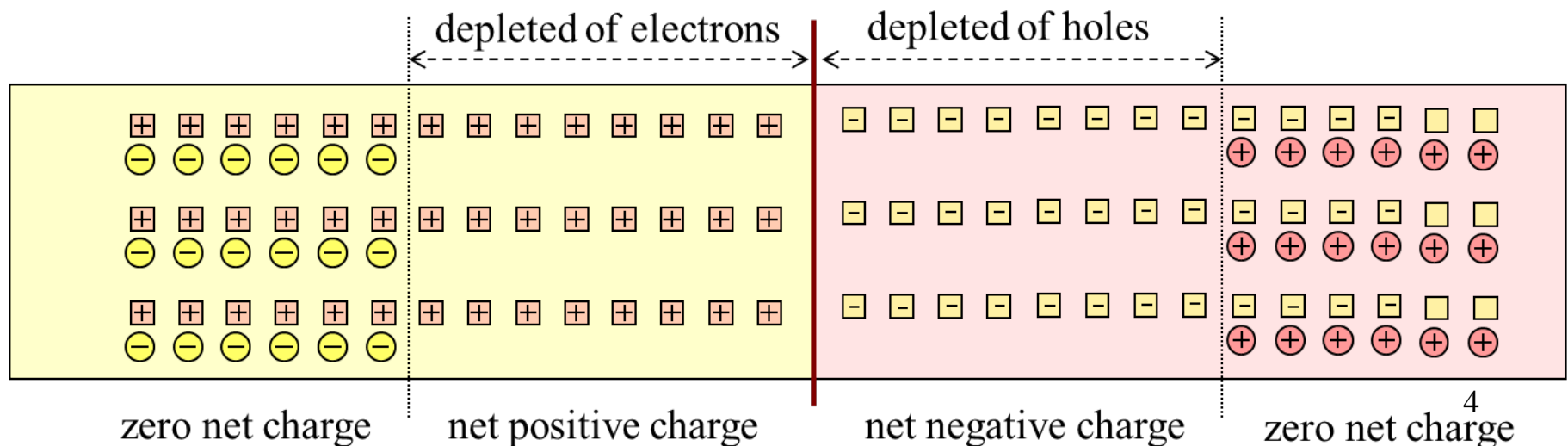
Electrons diffuse to right and recombine with holes



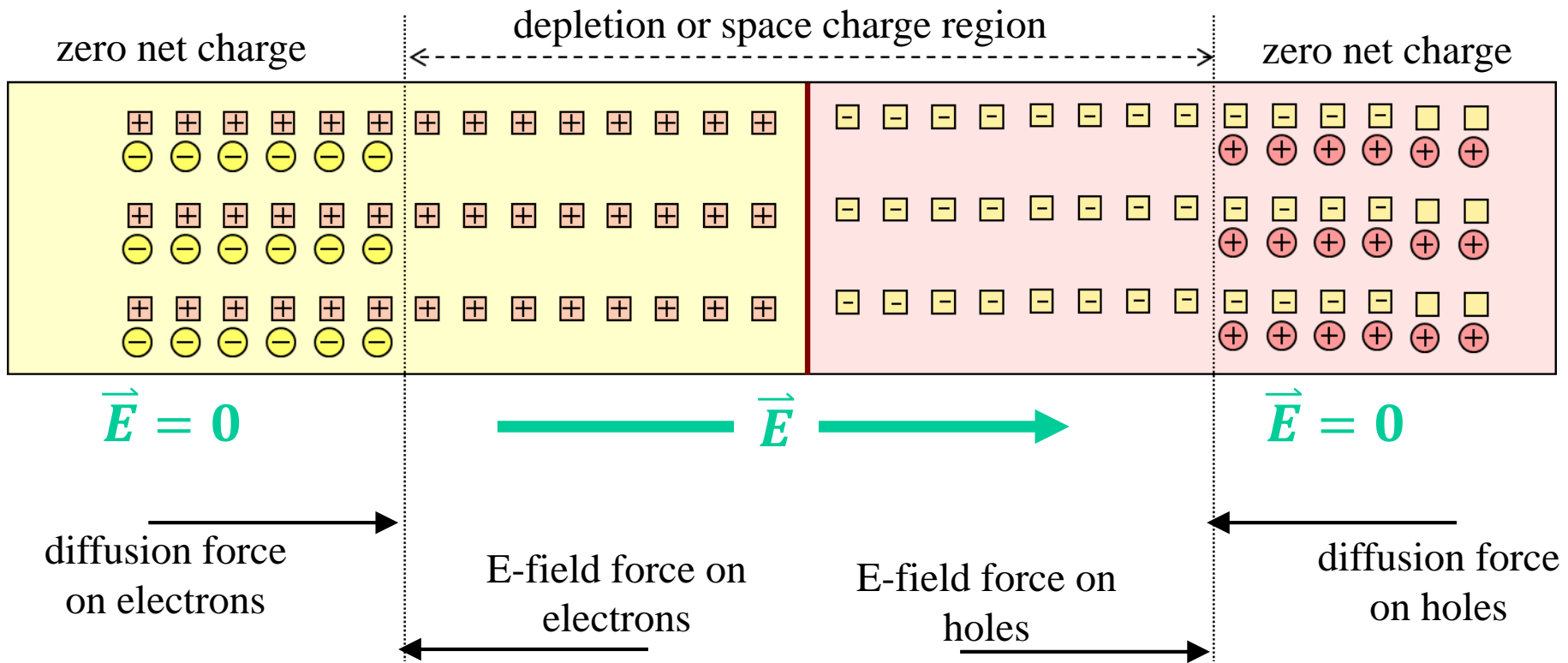
Holes diffuse to left and recombine with electrons



Leaving charged region of ionized donors:



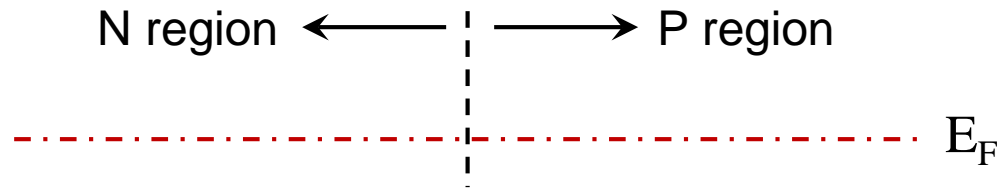
# Electric Field in Depletion Region



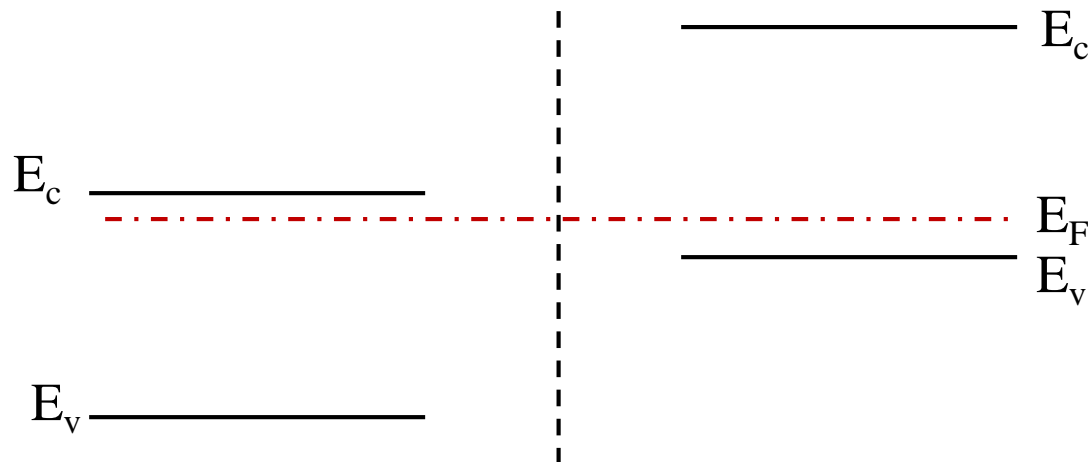
- Net positive and negative charges induce electric field
- Electric field pulls carriers in opposite direction to diffusion
- In thermal equilibrium, carriers diffuse until electric field exactly balances diffusion force

# Energy Band Diagram – Zero Bias

- Under zero external bias, junction is in thermal equilibrium
  - one Fermi level throughout device

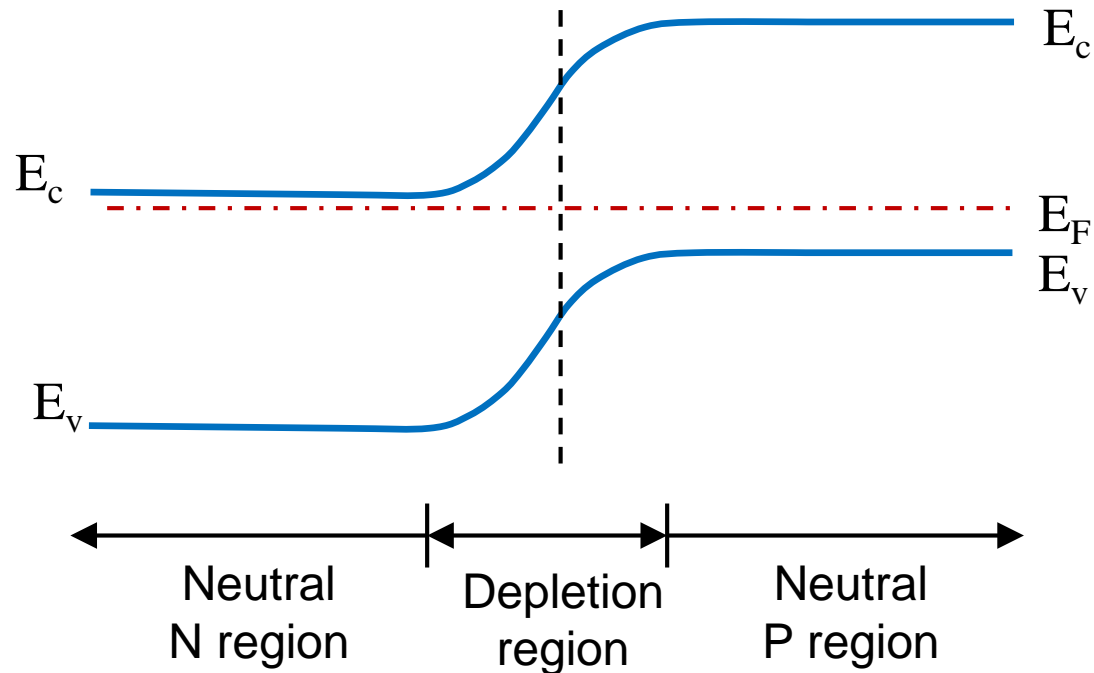


- Far from the junction, we have N-type (with  $E_c$  close to  $E_F$ ) and P-type (with  $E_v$  close to  $E_F$ )



# Energy Band Diagram – Depletion Region

- Within depletion region, assume (for now) that conduction & valence energies joined by a smooth curve



- In depletion region,  $E_F$  is far from both  $E_c$  and  $E_v$

$n \approx 0$  and  $p \approx 0$  in depletion layer

# Built-In Potential

- $E_c$  and  $E_v$  are not flat – indicates a potential difference
- This voltage differential  $\phi_{bi}$  is called built-in potential
  - exists at interface of any two dissimilar metals

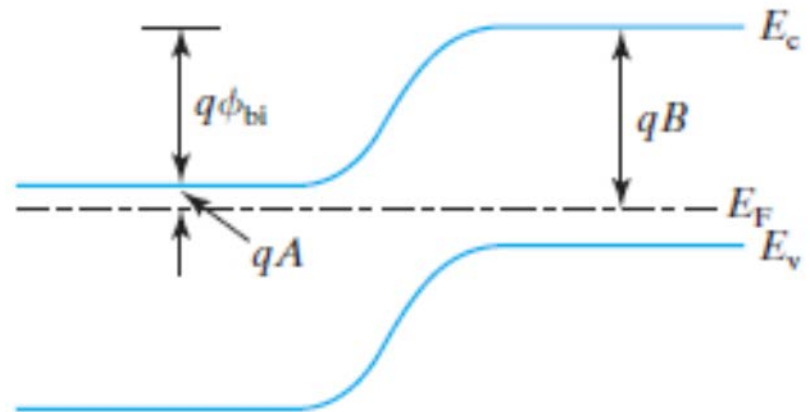
- In N-region:

$$n = N_d = N_c \cdot e^{-qA/kT}$$

$$A = \frac{kT}{q} \cdot \ln \left( \frac{N_c}{N_d} \right)$$

- In P-region:

$$n = \frac{n_i^2}{N_a} = N_c \cdot e^{-qB/kT}$$



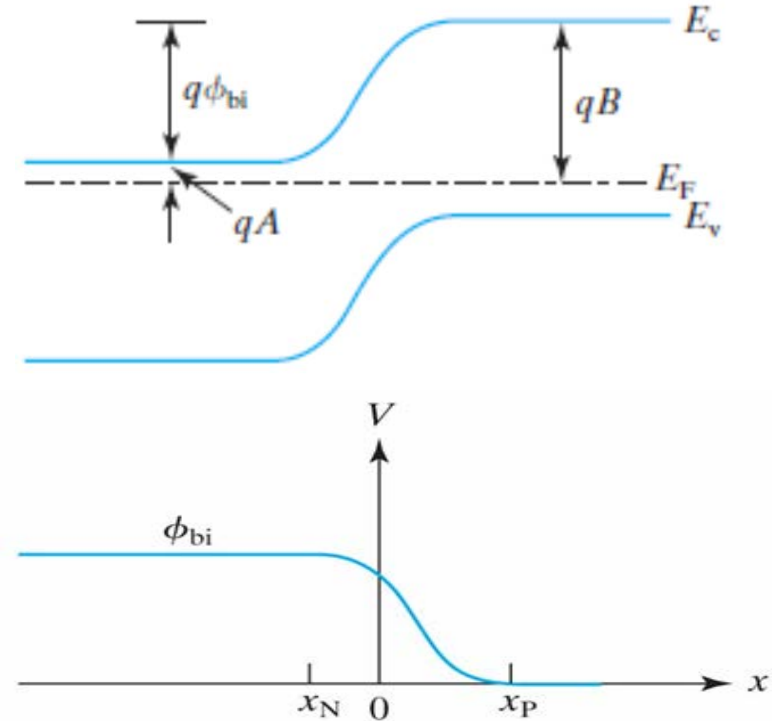
$$B = \frac{kT}{q} \cdot \ln \left( \frac{N_c \cdot N_a}{n_i^2} \right)$$



# Calculating Built-In Potential

$$\begin{aligned}\phi_{bi} &= B - A \\ &= \frac{kT}{q} \cdot \left[ \ln \left( \frac{N_c \cdot N_a}{n_i^2} \right) - \ln \left( \frac{N_c}{N_d} \right) \right]\end{aligned}$$

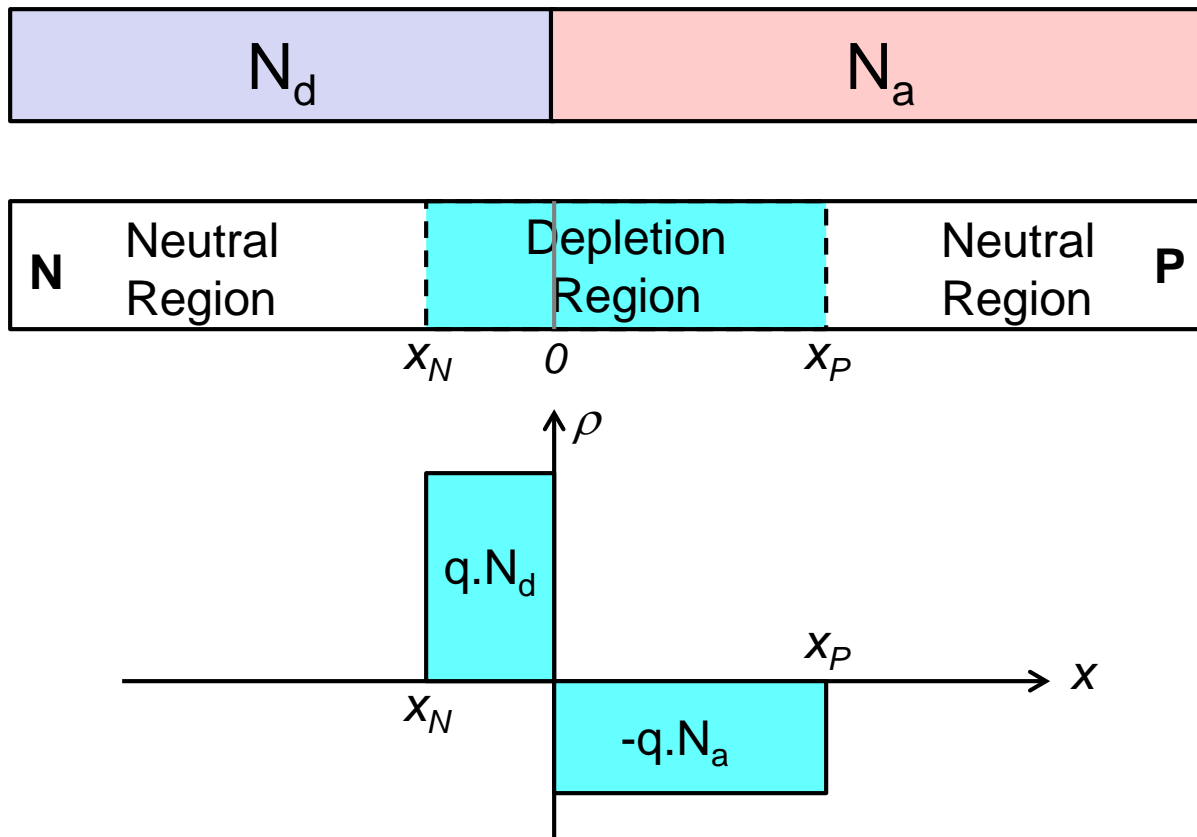
$$\phi_{bi} = \frac{kT}{q} \cdot \ln \left( \frac{N_d \cdot N_a}{n_i^2} \right)$$



- Typically  $\phi_{bi} \approx 0.7V - 0.9V$  in silicon
- Can we measure this with a voltmeter ?
- Why does this not generate drift current?

# Depletion Layer Model

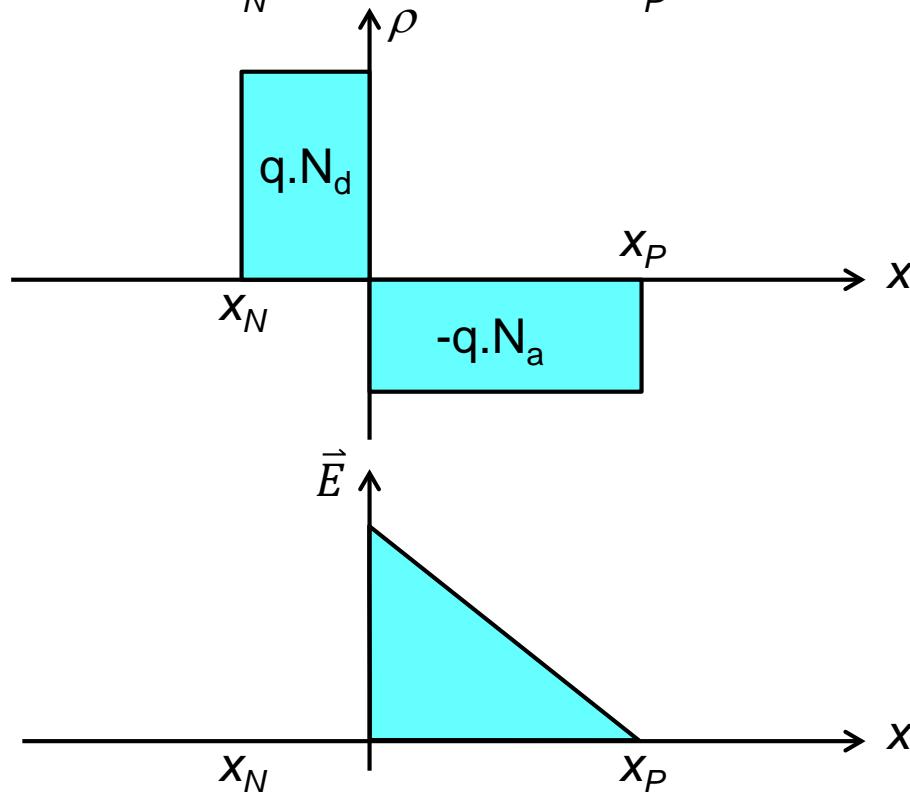
- Divide step PN junction into three regions
- Assume that  $p = n = 0$  in depletion region
  - charge density  $\rho$  equals dopant ion density in depletion region
  - charge density  $\rho = 0$  in neutral regions



# Poisson's Equation

- Poisson's Equation:

$$\frac{d^2V}{dx^2} = -\frac{d\vec{E}}{dx} = -\frac{\rho}{\epsilon_s}$$



- On P side of depletion region:

$$\rho = -q \cdot N_a \quad \Rightarrow \quad \frac{d\vec{E}}{dx} = -\frac{q \cdot N_a}{\epsilon_s}$$

$$\vec{E}(x) = -\frac{q \cdot N_a}{\epsilon_s} \cdot x + const.$$

- Setting  $\vec{E}(x_P) = 0$ , gives

$$\vec{E}(x) = \frac{q \cdot N_a}{\epsilon_s} \cdot (x_P - x) \quad 0 \leq x \leq x_P$$

# Electric Field

- Similarly, on N side of depletion region:

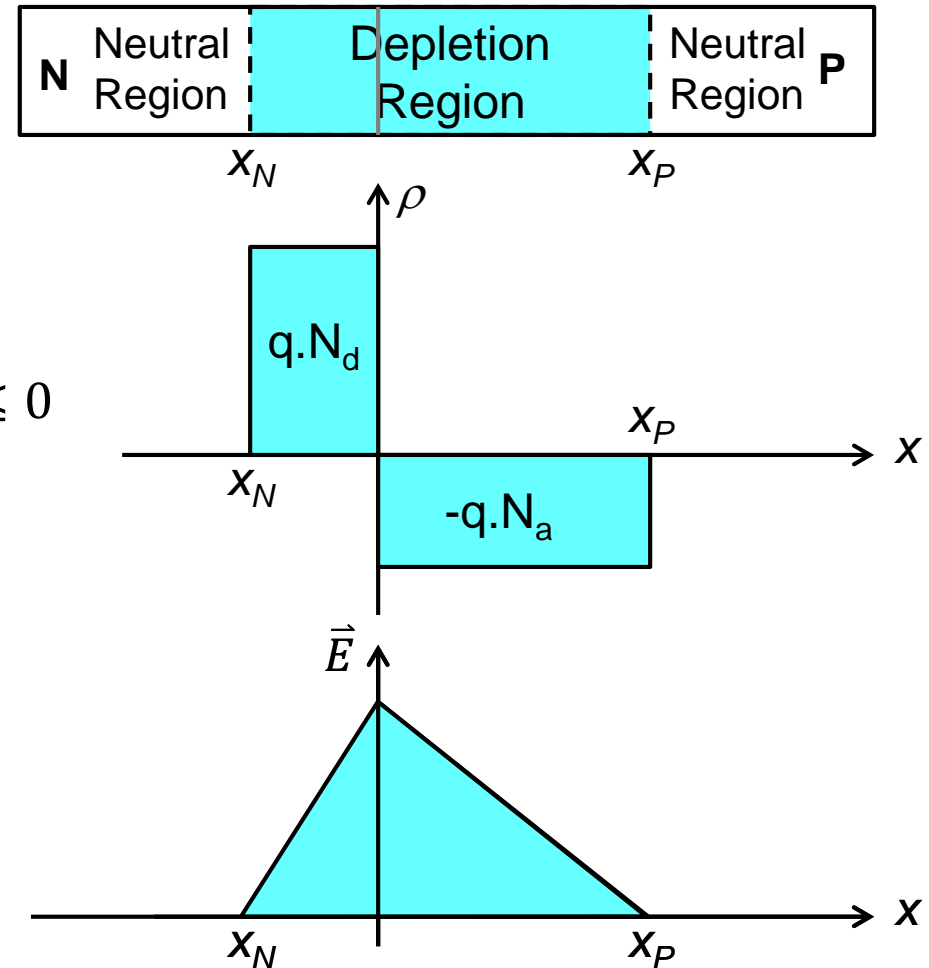
$$\rho = q \cdot N_d \quad \Rightarrow \quad \frac{d\vec{E}}{dx} = \frac{q \cdot N_d}{\epsilon_s}$$

$$\vec{E}(x) = \frac{q \cdot N_d}{\epsilon_s} \cdot (x - x_N) \quad x_N \leq x \leq 0$$

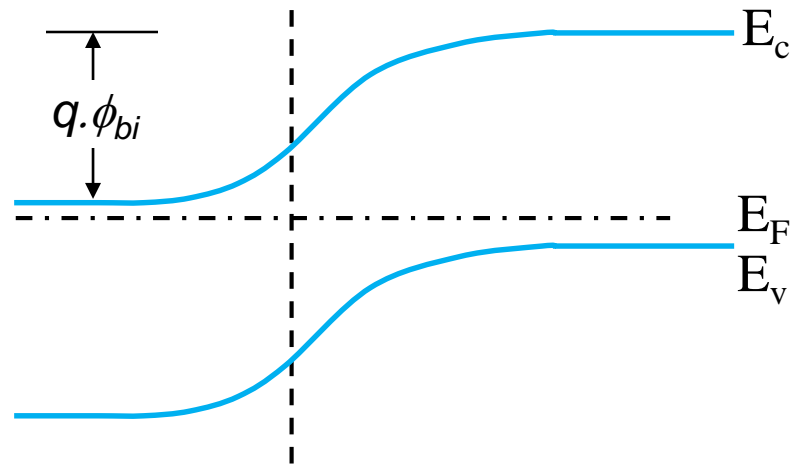
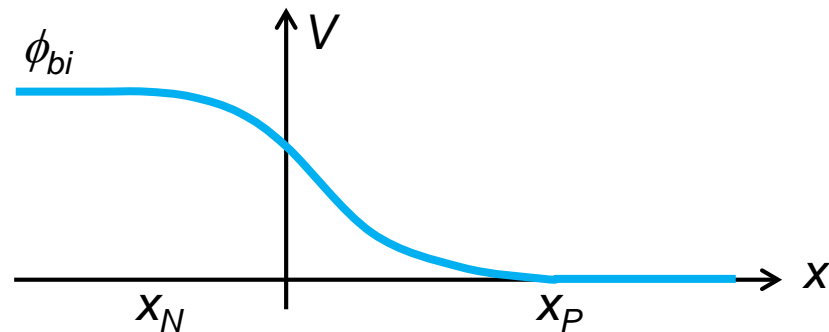
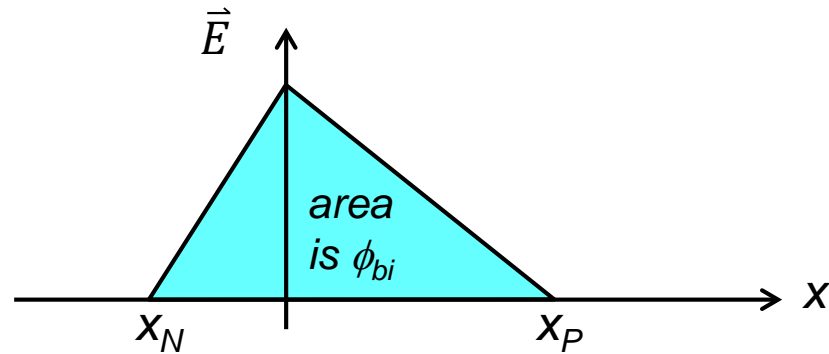
- Equating P side and N side fields at  $x=0$ :

$$N_a \cdot |x_P| = N_d \cdot |x_N|$$

- Depletion region extends further into more lightly doped side
- A highly asymmetrical junction (N<sup>+</sup>P or P<sup>+</sup>N) is called one-sided junction



# Potential in the Depletion Region



- On P-side: using  $\vec{E} = -dV/dx$  and integrating expressions for electric field and arbitrarily setting  $V(x_P) = 0$

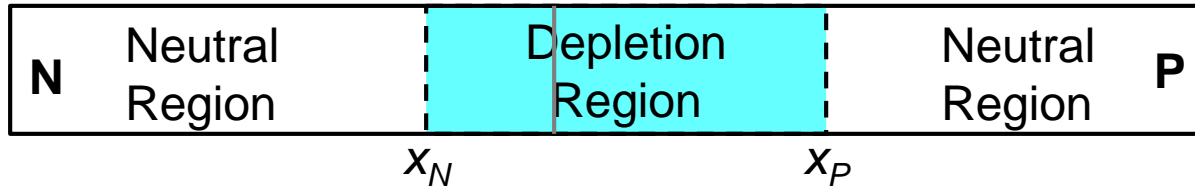
$$V(x) = \frac{q \cdot N_a}{2\epsilon_s} (x_P - x)^2 \quad 0 \leq x \leq x_P$$

- Similarly, on N-side, and setting  $V(x_N) = \phi_{bi}$

$$V(x) = \phi_{bi} - \frac{q \cdot N_d}{2\epsilon_s} (x - x_N)^2 \quad \text{for } x_N \leq x \leq 0$$

- Can now quantitatively draw energy band diagram

# Depletion Layer Width



- Equating N and P side potentials at  $x=0$ , gives:

$$x_P - x_N = W_{dep} = \sqrt{\frac{2\varepsilon_s \cdot \phi_{bi}}{q} \left( \frac{1}{N_a} + \frac{1}{N_d} \right)}$$

- If  $N_a \gg N_d$ , as in a P+N junction

$$W_{dep} \approx \sqrt{\frac{2\varepsilon_s \cdot \phi_{bi}}{q \cdot N_d}} \approx |x_N|$$

- Similarly, if  $N_d \gg N_a$  as in N+P junction:

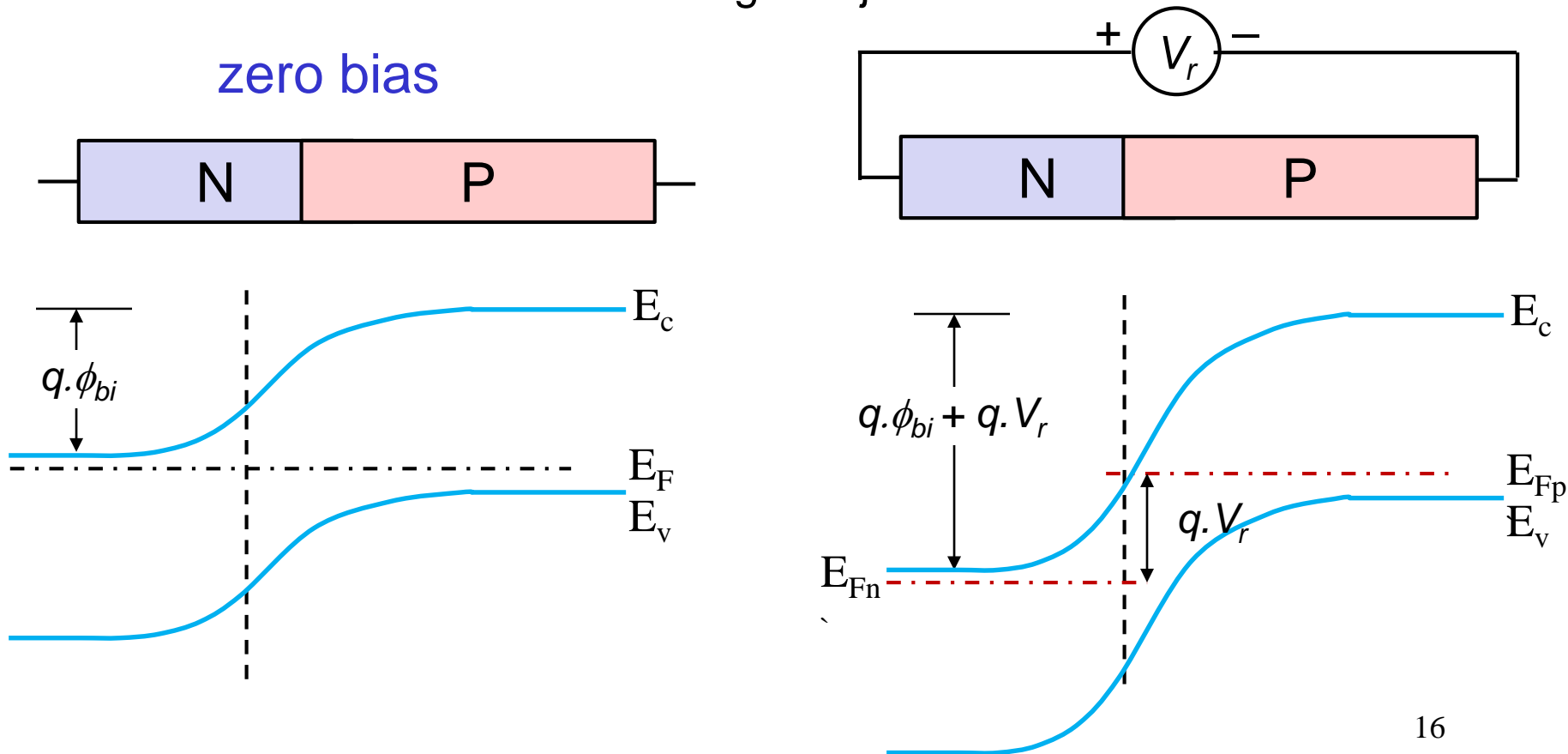
$$W_{dep} \approx \sqrt{\frac{2\varepsilon_s \cdot \phi_{bi}}{q \cdot N_a}} \approx |x_P|$$

## Example: PN Junction

- A P+N junction has  $N_a = 10^{19} \text{cm}^{-3}$  and  $N_d = 10^{16} \text{cm}^{-3}$  .  
What is (a) the built-in potential, (b)  $W_{\text{dep}}$ , (c)  $x_N$  and (d)  $x_P$  ?

# Reverse Biased PN Junction

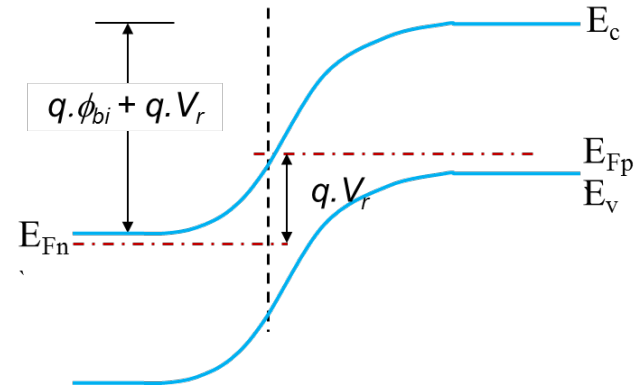
- When a positive voltage is applied to N region relative to P region, the PN junction is said to be **reverse biased**
- No longer in thermal equilibrium
  - Fermi level not constant throughout junction





# Reverse Biased Depletion Width

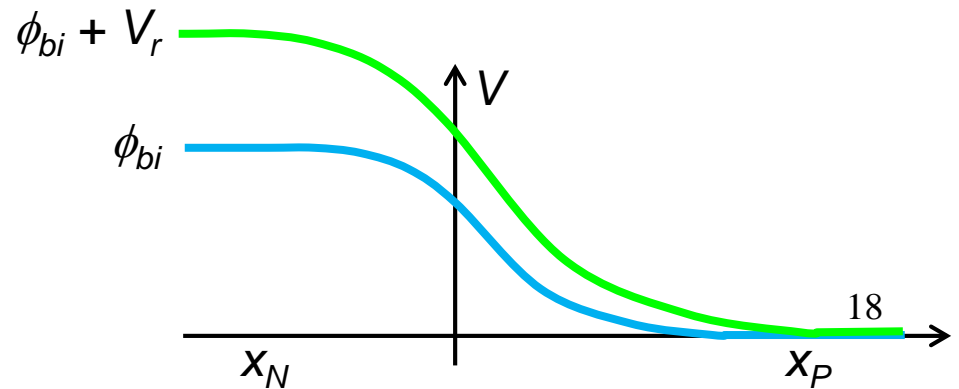
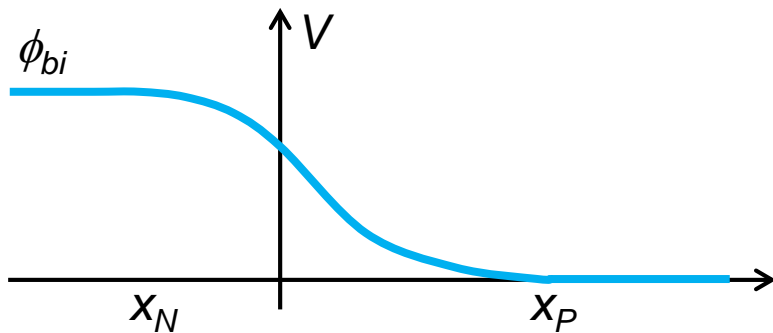
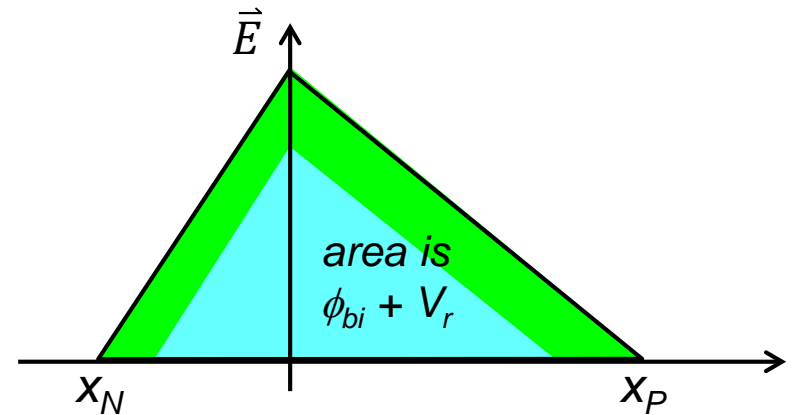
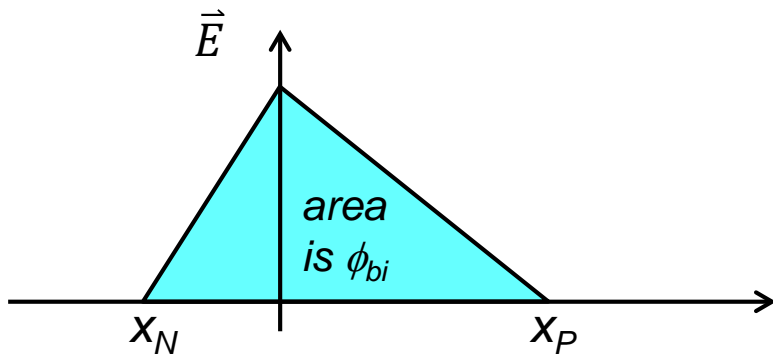
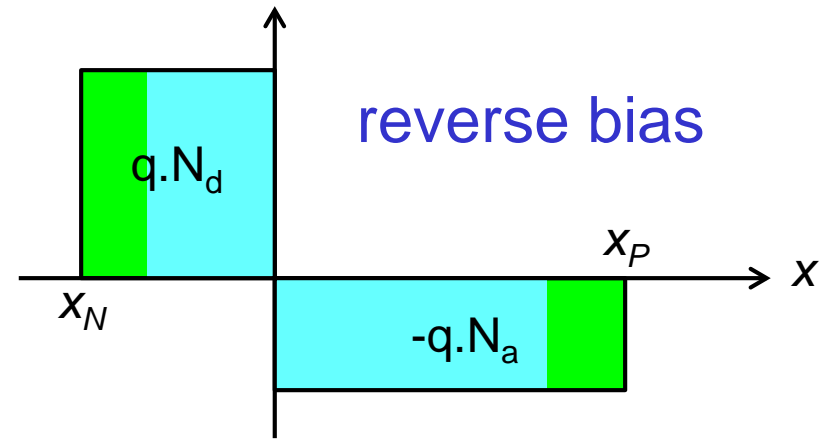
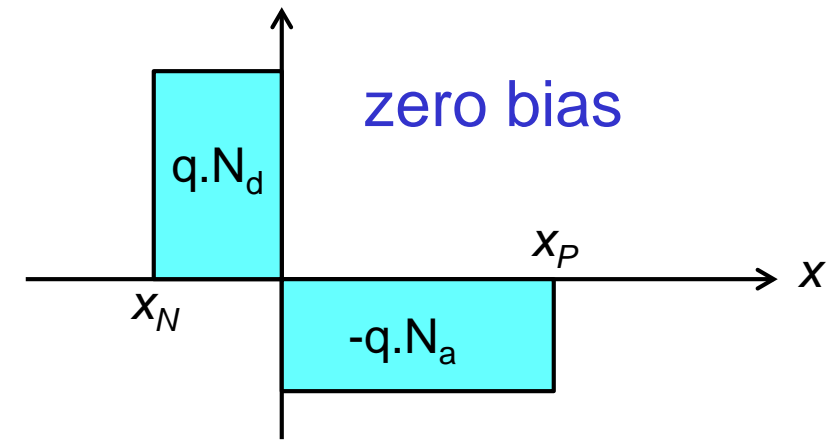
- Potential barrier to flow of majority carriers has increased from  $\phi_{bi}$  to  $(\phi_{bi} + V_r)$
- Reverse biased current is very small
  - Due to minority carriers in N and P sections
  - *Since current is small:*
- IR drop in neutral regions is negligible
  - All reverse bias appears across depletion region
- Analysis using Poisson's equation (at thermal equilibrium) is still valid if the  $\phi_{bi}$  term is replaced with  $(\phi_{bi} + V_r)$



$$W_{dep} = \sqrt{\frac{2\epsilon_s(\phi_{bi} + V_r)}{q \cdot N}} = \sqrt{\frac{2\epsilon_s \times \text{potential barrier}}{q \cdot N}}$$

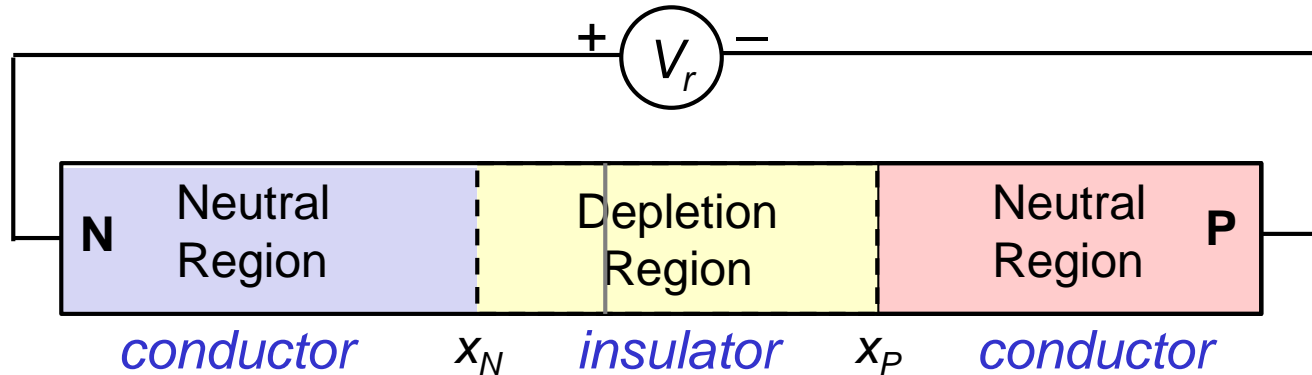
where  $\frac{1}{N} = \frac{1}{N_d} + \frac{1}{N_a} \approx \frac{1}{\text{lighter dopant density}}$

# Reverse Biased Field & Potential

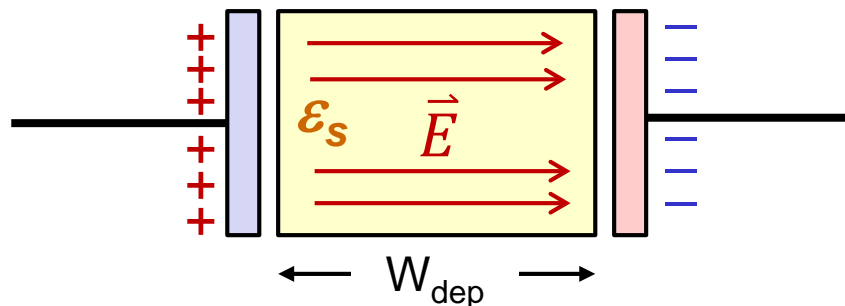


# Capacitance Model

- Two neutral regions separated by depletion region can be viewed as two conductors separated by an insulator



- PN Junction can be modeled as parallel plate capacitor



$$C_{dep} = \frac{\epsilon_s \cdot A}{W_{dep}}$$

# Capacitance Values

$$C_{dep} = \frac{\epsilon_s \cdot A}{W_{dep}}$$

- Substituting for  $W_{dep}$  gives:

$$C_{dep} = A \cdot \sqrt{\frac{q \cdot N \cdot \epsilon_s}{2(\phi_{bi} + V_r)}}$$

*remember:*

$$\frac{1}{N} = \frac{1}{N_A} + \frac{1}{N_D}$$

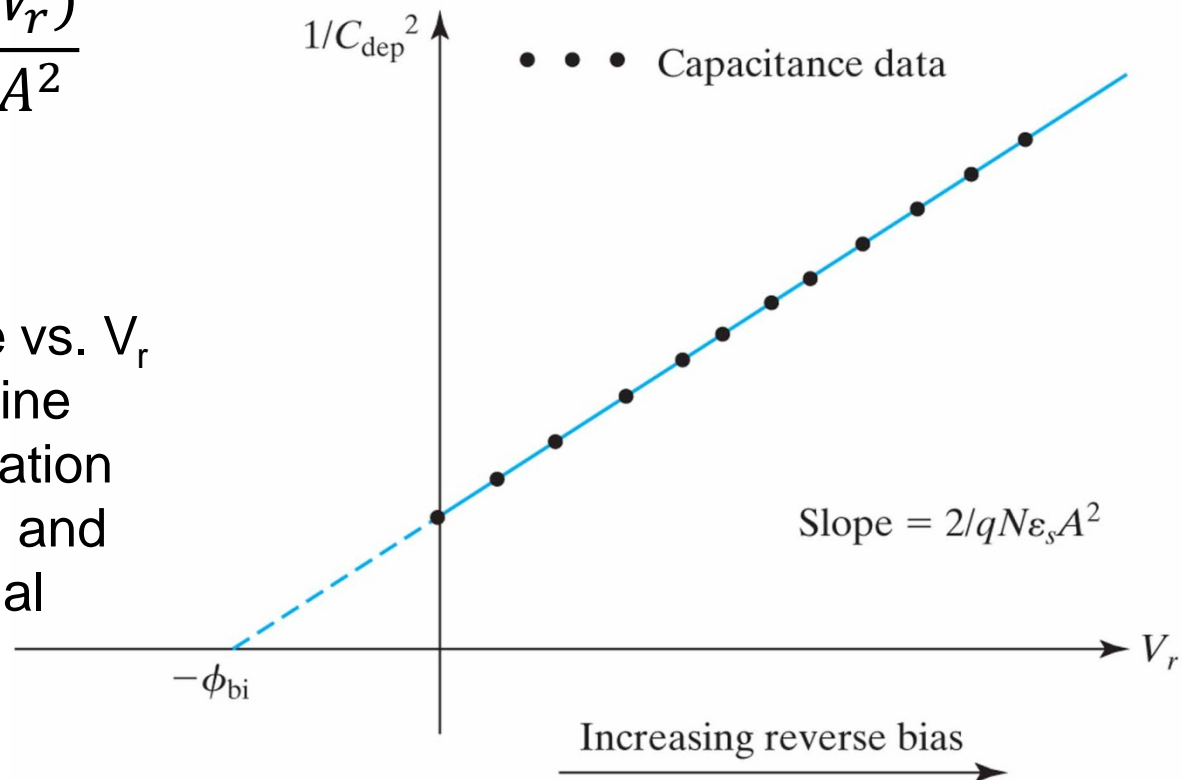
- $C_{dep}$  increases with doping concentration in more lightly doped side
- $C_{dep}$  decreases as applied reverse bias increases
- $C_{dep}$  is important as PN junctions are present in most semiconductor devices

# Capacitance-Voltage Characteristic

- rewriting capacitance expression:

$$\frac{1}{C_{dep}^2} = \frac{2(\phi_{bi} + V_r)}{q \cdot N \cdot \epsilon_s \cdot A^2}$$

- Measured capacitance vs.  $V_r$  can be used to determine lighter doped concentration in a one-sided junction and also the built-in potential

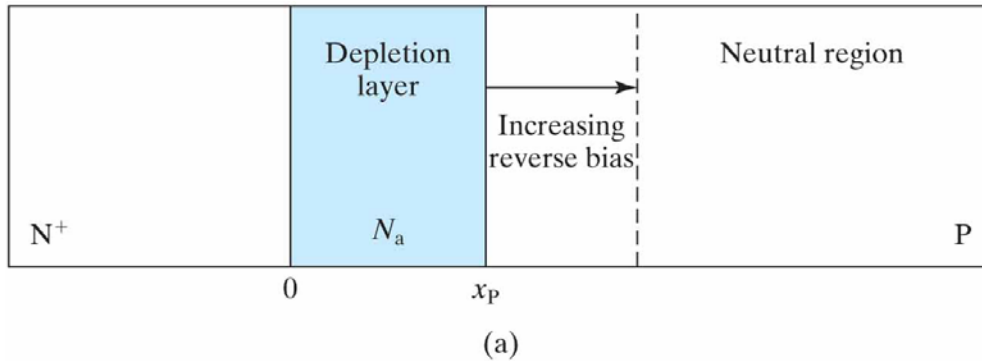


## Example: C-V data

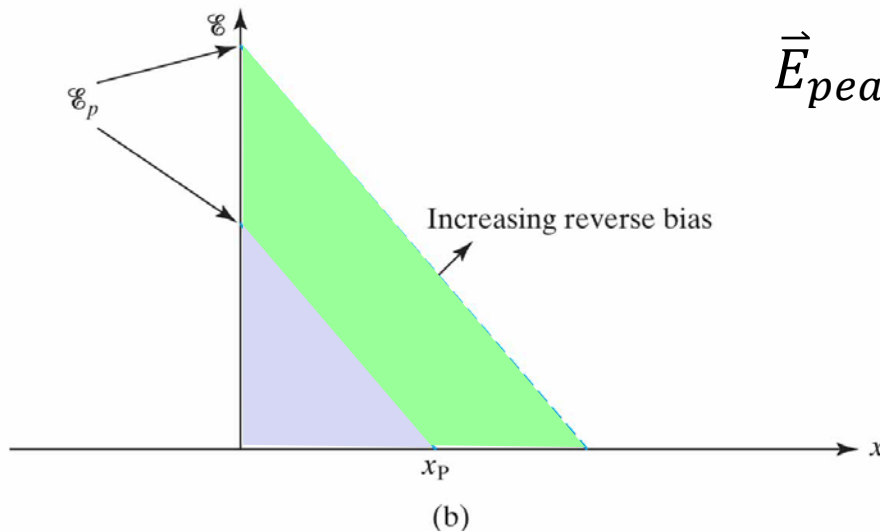
- The measured slope of the  $1/C^2$  vs.  $V_r$  plot for a PN diode is  $2 \times 10^{31} F^{-2}V^{-1}$  and the intercept is at  $-0.84 V$ . The area of the PN junction is  $1 \mu m^2$ . Find the lighter doping concentration  $N_l$  and the heavier doping concentration  $N_h$ . (*Accuracy?*)

# Peak Electric Field

- Under moderate bias reverse current negligibly small
- As reverse bias is increased, peak electric field increases:

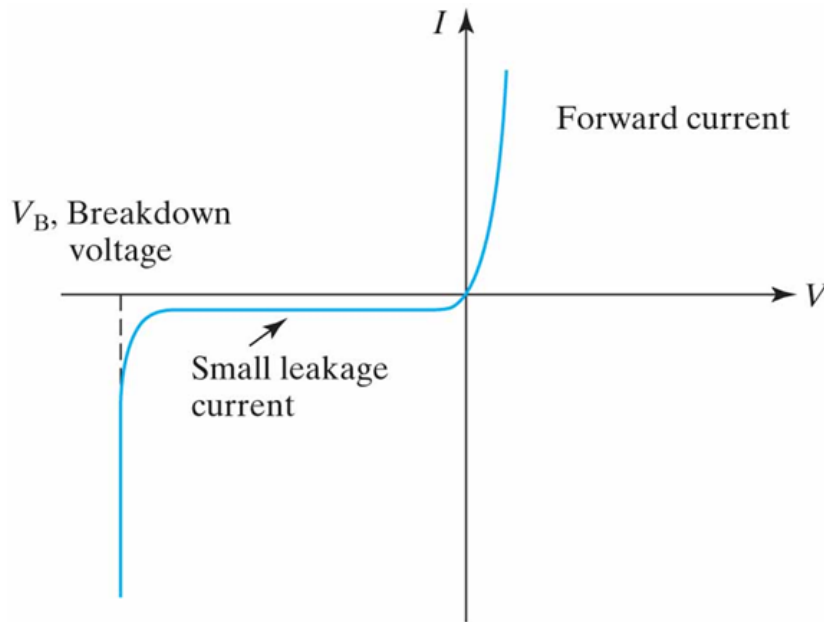


$$\vec{E}_{peak} = \vec{E}(0) = \left[ \frac{2q \cdot N}{\epsilon_s} (\phi_{bi} + V_r) \right]^{1/2}$$



# Junction Breakdown

- When electric field reaches critical value  $\vec{E}_{crit}$  junction will break down and conduct large current



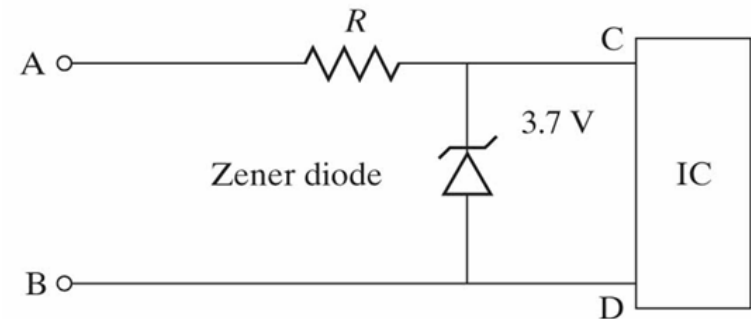
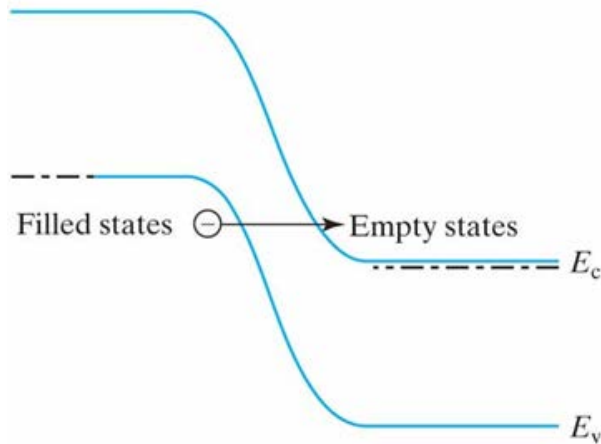
$$V_B = \frac{\epsilon_s \cdot \vec{E}_{crit}^2}{2q \cdot N} - \phi_{bi}$$

- Two types of breakdown:
  - Tunneling (or Zener) breakdown in heavily doped junctions
  - Avalanche breakdown in moderately doped junctions



# Tunneling (Zener) Breakdown

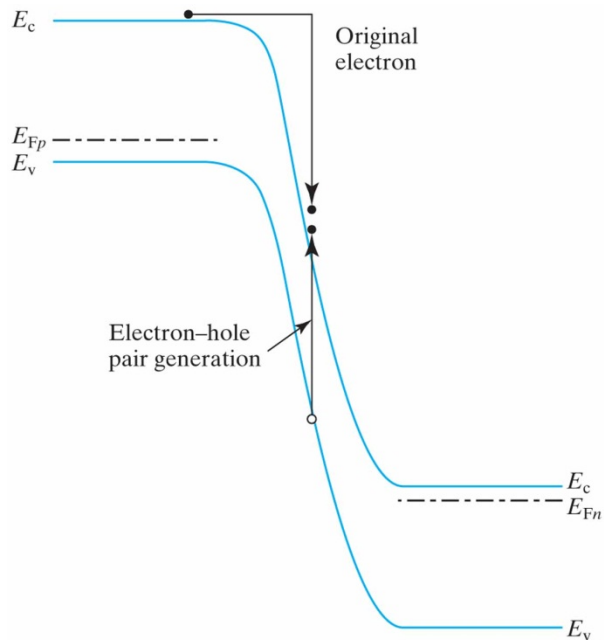
- When heavily doped junction is reverse biased, only a small distance separates electrons in P-side valence band from empty states in N-side conduction band:



- Electrons can “tunnel” across junction
  - $\vec{E}_{crit} \approx 10^6 \text{ volts/cm}$
  - Breakdown is not destructive as long as current is controlled
  - Zener diodes operate in this mode with well controlled  $V_B$

# Avalanche Breakdown

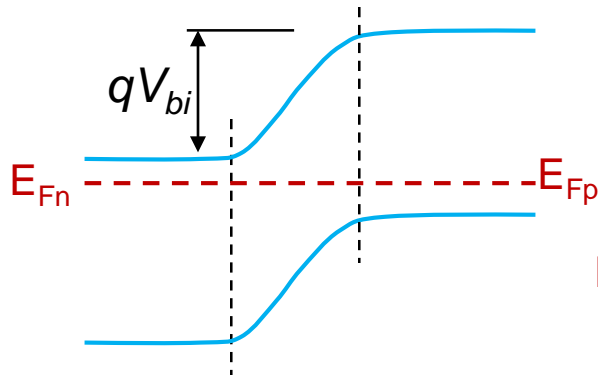
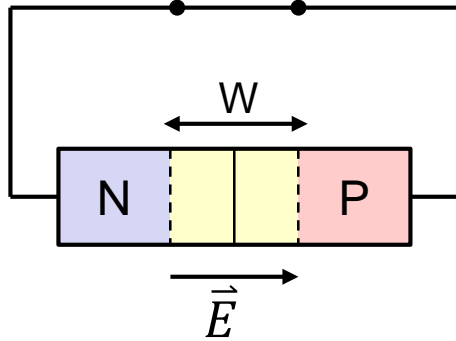
- In moderately doped junctions, high electric fields cause minority carriers to accelerate across depletion region
- They may gain enough kinetic energy to raise an electron from the valence band to conduction band (impact ionization)
  - creates an extra electron-hole pair which will also be accelerated
- Extra carriers collide with lattice and create still more carriers
  - avalanche effect



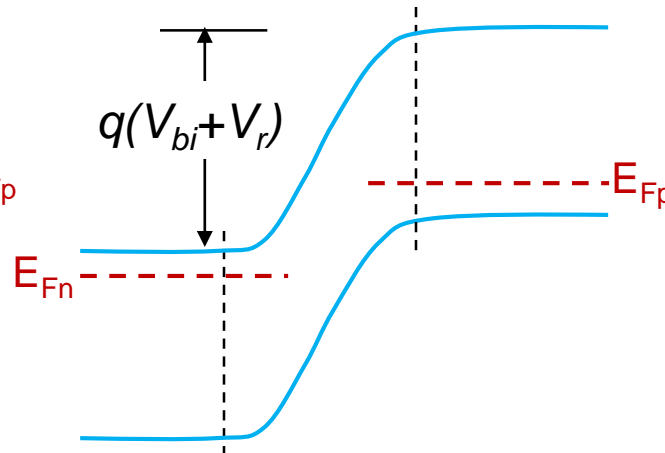
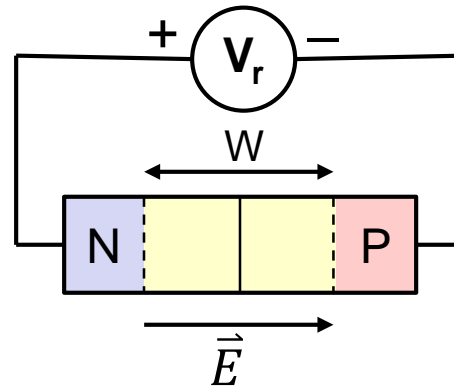
- $\vec{E}_{crit} \approx 5 \times 10^5 \text{ V/cm}$  at  $N = 10^{17} \text{ cm}^{-3}$
- $V_B \approx 15 \text{ V}$  at  $N = 10^{17} \text{ cm}^{-3}$

# Forward Biased Junction

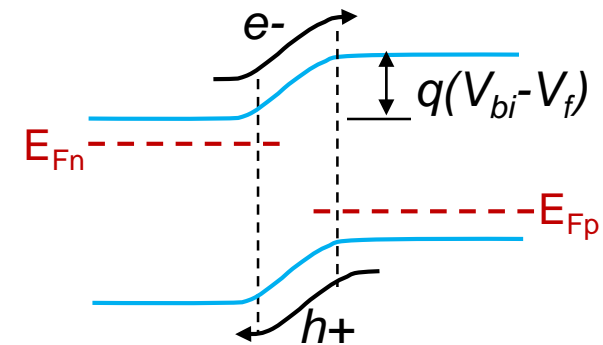
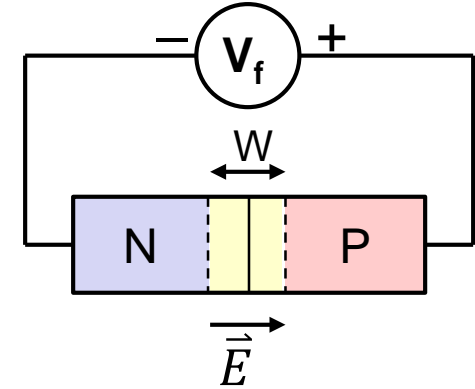
zero bias



reverse bias



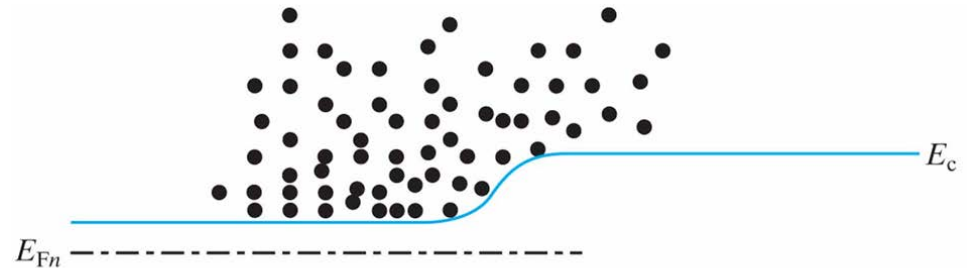
forward bias



- Reduced electric field allows electrons to diffuse from N to P
  - and holes to diffuse from P to N
  - known as minority carrier injection

# Minority Carrier Injection

- Forward bias of  $V$  reduces barrier height from  $\phi_{bi}$  to  $\phi_{bi} - V$
- Upsets balance between drift and diffusion
- Electrons are injected into P-side, holes into N-side
- Assuming  $E_{Fn}$  remains constant through to  $x_P$ , at edge of neutral P region:

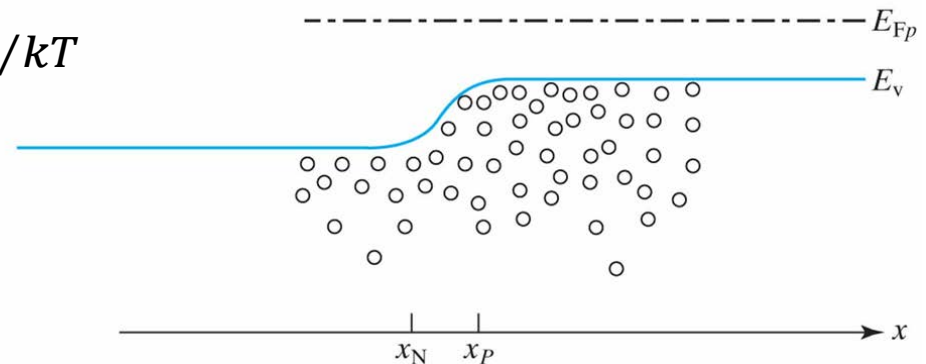


$$n(x_P) = N_C \cdot e^{-(E_C - E_{Fn})/kT}$$

$$= N_C \cdot e^{-(E_C - E_{Fp})/kT} \cdot e^{(E_{Fn} - E_{Fp})/kT}$$

$$= n_{P0} \cdot e^{(E_{Fn} - E_{Fp})/kT}$$

$$= n_{P0} \cdot e^{qV/kT}$$



# Quasi-Equilibrium Boundary Condition

- Minority carrier density in neutral region at the edge of depletion region is raised by  $e^{qV/kT}$

$$n(x_P) = n_{P0} \cdot e^{qV/kT} = \frac{n_i^2}{N_a} e^{qV/kT}$$
$$p(x_N) = p_{N0} \cdot e^{qV/kT} = \frac{n_i^2}{N_d} e^{qV/kT}$$

- Rewriting in terms of excess minority carriers:

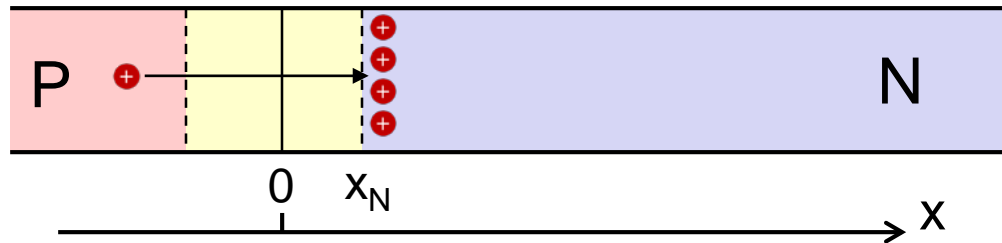
$$n'(x_P) \equiv n(x_P) - n_{P0} = n_{P0} \cdot (e^{qV/kT} - 1)$$
$$p'(x_N) \equiv p(x_N) - p_{N0} = p_{N0} \cdot (e^{qV/kT} - 1)$$

- In Si at 300°K, a forward bias of 0.6V raises minority carrier density by a factor of  $10^{10}$  !

# Example: Carrier Injection

- A P+N junction has  $N_a = 10^{18} \text{cm}^{-3}$  and  $N_d = 10^{16} \text{cm}^{-3}$ .
  - a) What are the minority carrier densities at the depletion region edges at zero bias?
  - b) What are the minority carrier densities at the depletion region edges with a forward bias of  $0.6\text{V}$ ?
  - c) What are the excess minority carrier densities at the depletion region edges with a forward bias of  $0.6\text{V}$ ?
  - d) What are the majority carrier densities at the depletion region edges with a forward bias of  $0.6\text{V}$ ?
  - e) What are the minority carrier densities at the depletion region edges with a negative bias of  $1.8\text{V}$ ?

# Carrier Transport in Neutral Region



- Consider transport of minority holes in neutral N region
- Apply diffusion equation (Lecture 4) under the conditions:
  - steady state
  - constant doping (in neutral region)
  - negligible electric field

$$\frac{d^2 p'}{dx^2} = \frac{p'}{D_p \cdot \tau_p} = \frac{p'}{L_p^2}$$

where  $L_p \equiv \sqrt{D_p \cdot \tau_p}$

- $L_p$  is the minority carrier diffusion length

# Minority Carrier Diffusion Length

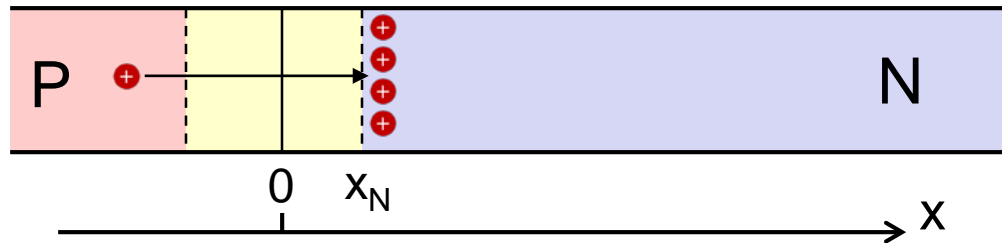
- Similarly, in the P neutral region:

$$\frac{d^2 n'}{dx^2} = \frac{n'}{L_n^2} \quad \text{where} \quad L_n \equiv \sqrt{D_n \cdot \tau_n}$$

- Minority carrier diffusion length is a measure of how far an injected minority carrier will travel before recombination
- Varies from few  $\mu\text{m}$  to hundreds of  $\mu\text{m}$  depending on  $\tau$
- Note that these equations are only valid for minority carriers
  - Cannot neglect drift in neutral region for majority carriers



# Excess Carriers in Forward Biased Junction



- We solve 
$$\frac{d^2 p'}{dx^2} = \frac{p'}{L_p^2}$$

with boundary conditions:

$$p'(\infty) = 0$$
$$p'(x_N) = p_{N0} (e^{qV/kT} - 1)$$

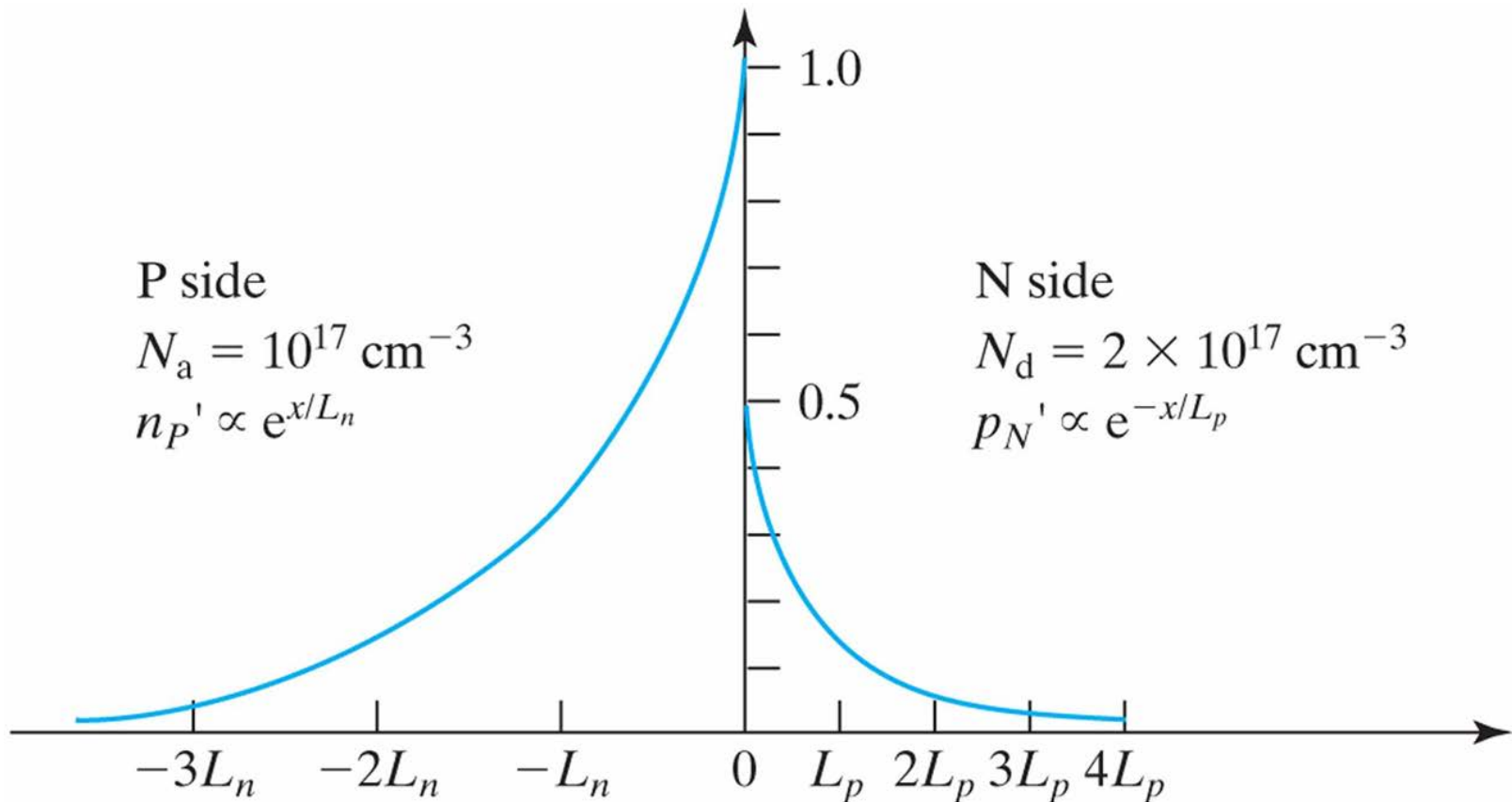
- General solution is 
$$p'(x) = A \cdot e^{x/L_p} + B \cdot e^{-x/L_p}$$
  - First boundary condition implies  $A=0$ , second determines  $B$ :

$$p'(x) = p_{N0} (e^{qV/kT} - 1) \cdot e^{-(x-x_N)/L_p}, \quad x > x_N$$

# Excess Carrier Distribution

$$p'(x) = p_{N0} (e^{qV/kT} - 1) \cdot e^{(x_N - x)/L_p}, \quad x > x_N$$

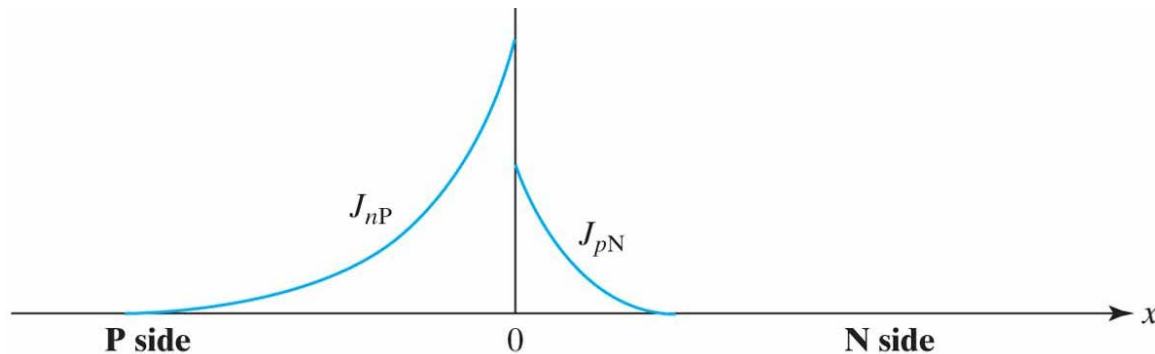
- Similarly:  $n'(x) = n_{P0} (e^{qV/kT} - 1) \cdot e^{(x - x_P)/L_n}, \quad x < x_P$



# Excess Minority Carrier Current

$$J_{pN} = -q \cdot D_p \frac{dp'(x)}{dx} = q \cdot \frac{D_p}{L_p} \cdot p_{N0} (e^{qV/kT} - 1) \cdot e^{-(x-x_N)/L_p}$$

$$J_{nP} = q \cdot D_n \frac{dn'(x)}{dx} = q \cdot \frac{D_n}{L_n} \cdot n_{P0} (e^{qV/kT} - 1) \cdot e^{(x-x_P)/L_n}$$

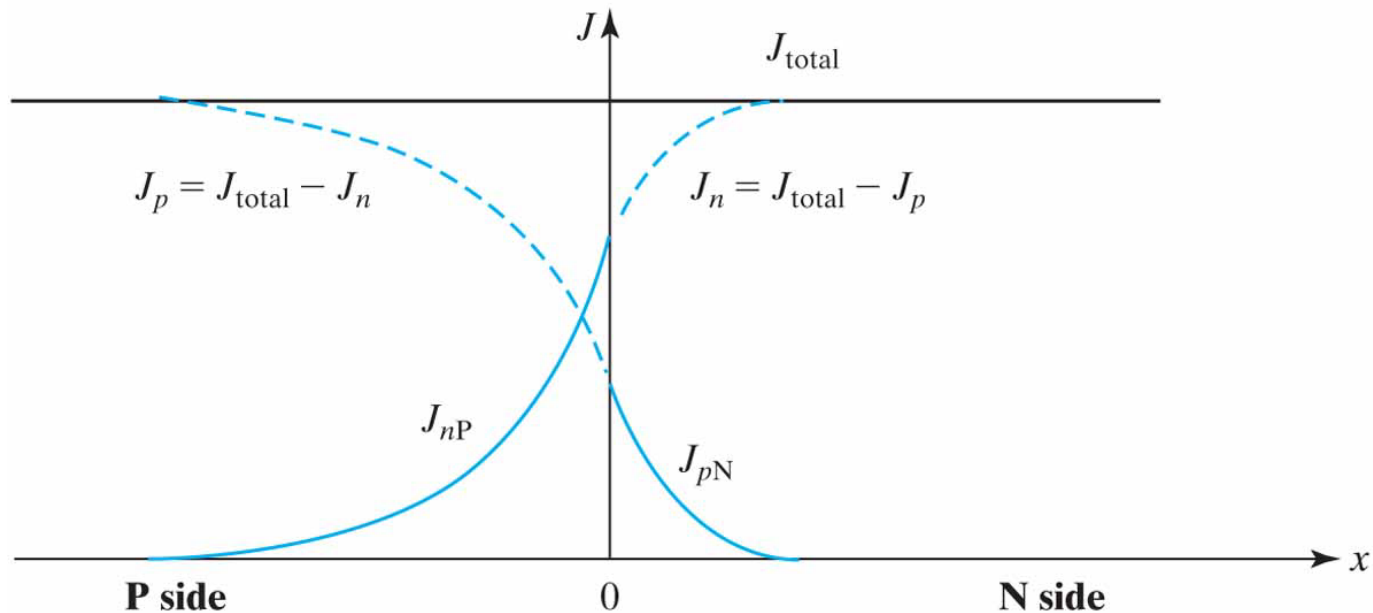


- At  $x=0$ , total current is due to injected minority carriers

$$J(0) = J_{pN}(x_N) + J_{nP}(x_P) = q \cdot \left( \frac{D_p}{L_p} \cdot p_{N0} + \frac{D_n}{L_n} \cdot n_{P0} \right) \cdot (e^{qV/kT} - 1)$$

# Majority Carrier Current

- Total current at  $x=0$  equals total current at all values of  $x$
- As minority carrier current density decreases leaving the depletion region boundary, majority carrier current density increases to keep the total current density constant

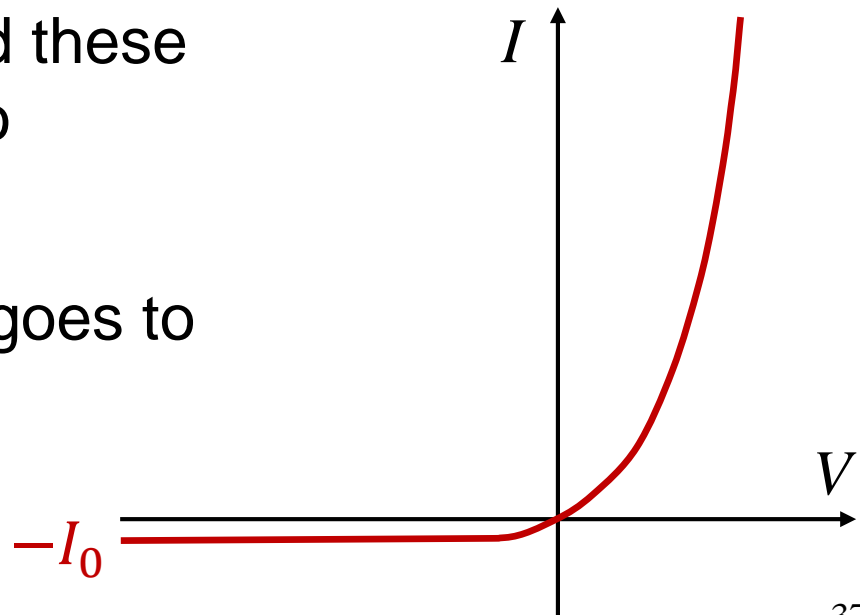


# PN Diode IV Characteristic

- Rewriting equation for total current density:

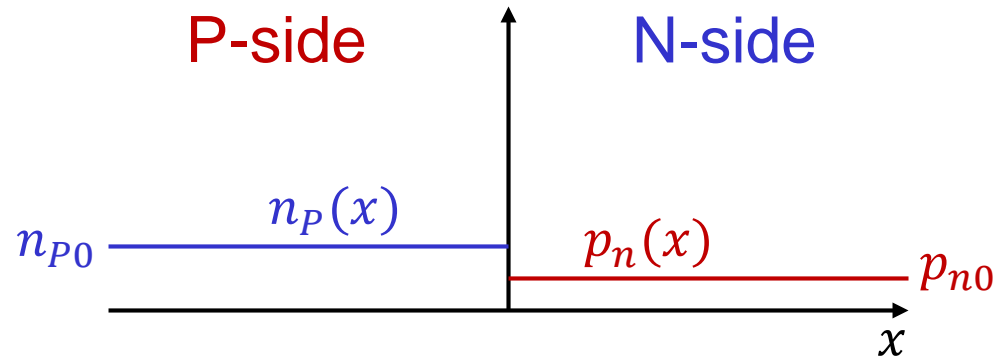
$$I = J \cdot A = I_0 (e^{qV/kT} - 1)$$
$$I_0 = A \cdot q \cdot n_i^2 \left( \frac{D_p}{L_p \cdot N_d} + \frac{D_n}{L_n \cdot N_a} \right)$$

- Note that our analysis and these equations apply equally to reverse bias ( $V < 0$ )
- For  $V_r \gg kT$ , exponential goes to zero and  $I = -I_0$   
(reverse saturation current)

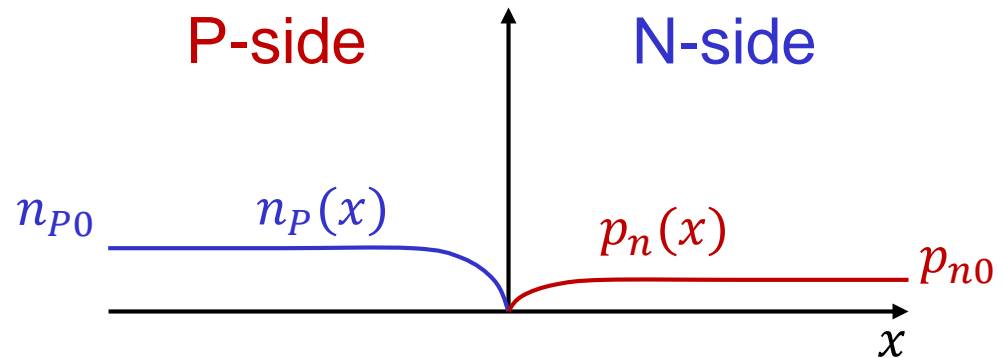


# Minority Carrier Concentrations

zero bias

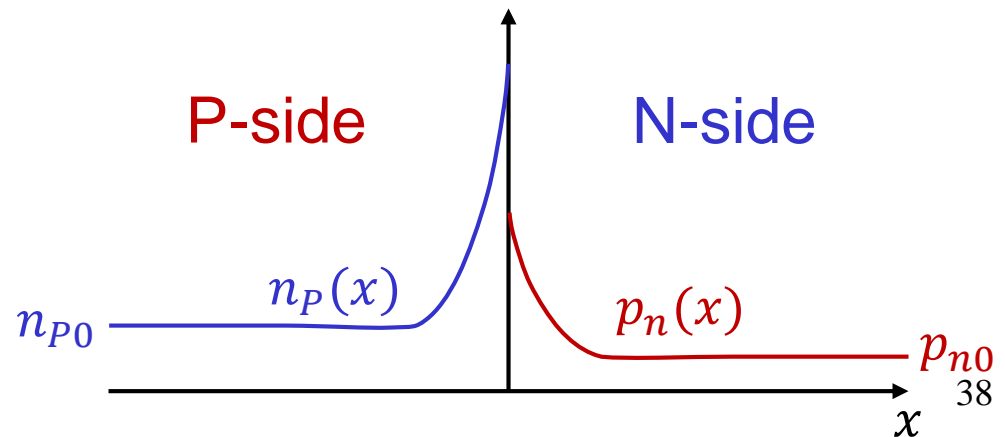


reverse bias

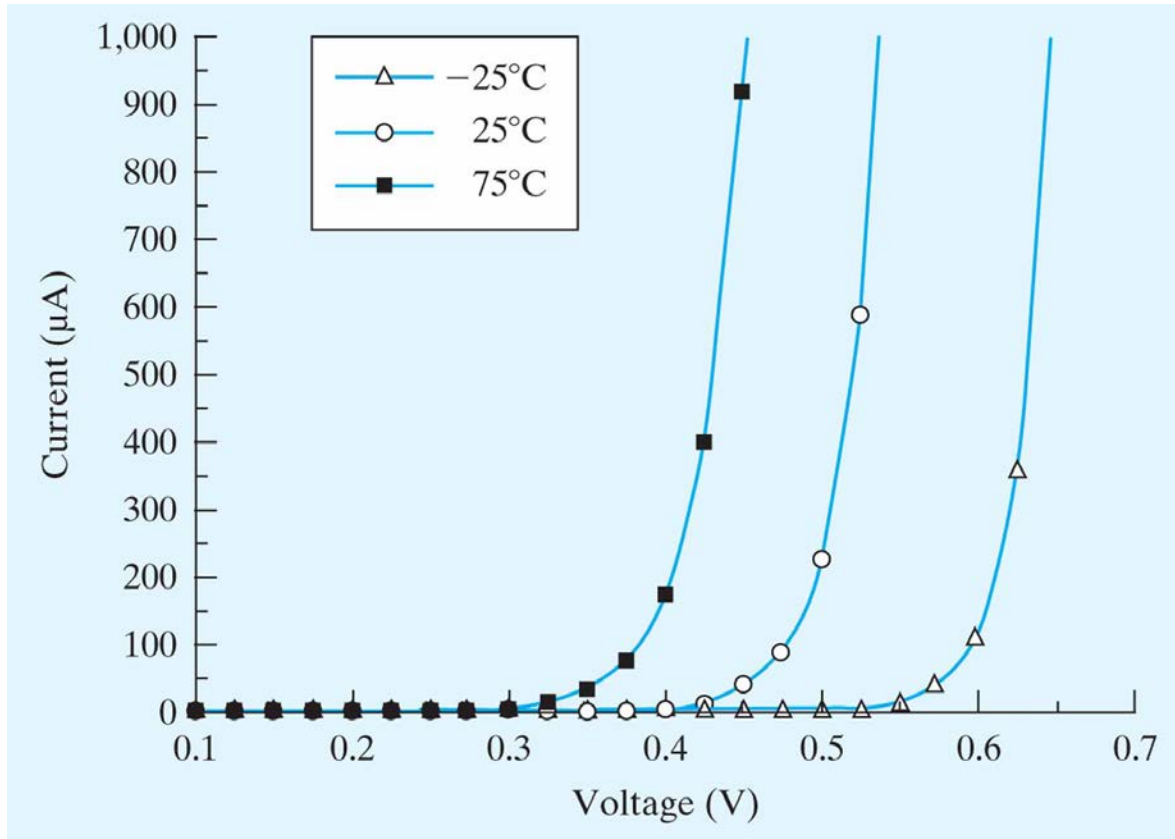


forward bias\*

\* in forward bias, injected majority carriers orders of magnitude greater than equilibrium concentration



# PN Diode IV vs. Temperature



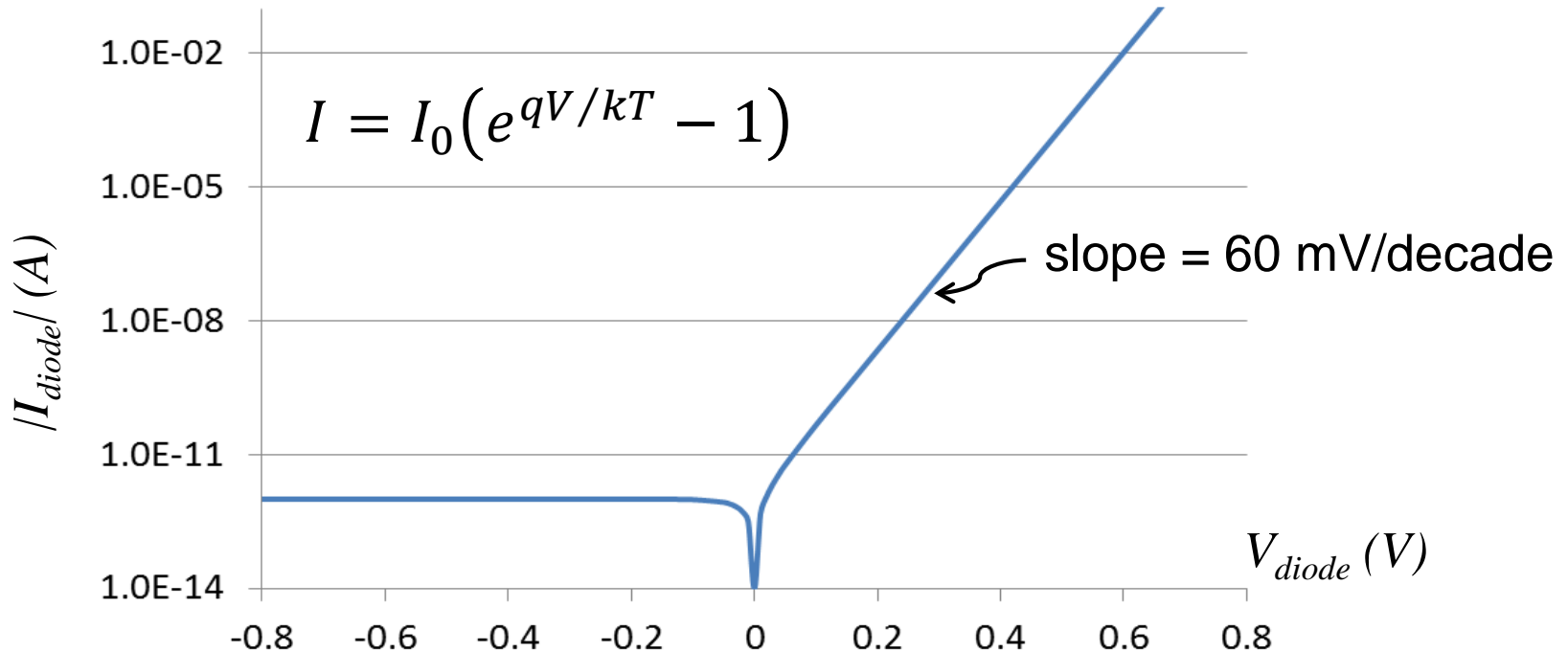
$$I = I_0(e^{qV/kT} - 1)$$

- Why does current increase with temperature?

$$I_0 = A \cdot q \cdot n_i^2 \left( \frac{D_p}{L_p \cdot N_d} + \frac{D_n}{L_n \cdot N_a} \right)$$

# Semi-log plot of IV for ideal diode

- Ideal diode characteristic for  $I_0 = 10^{-12}$  A and  $T=300^\circ\text{K}$



For  $V \gg kT$ ,  $\ln(I) = \ln(I_0) + \frac{qV}{kT}$

- plotting  $\ln(I)$  vs.  $V$ , slope =  $q/kT$
- diode can be used as temperature sensor



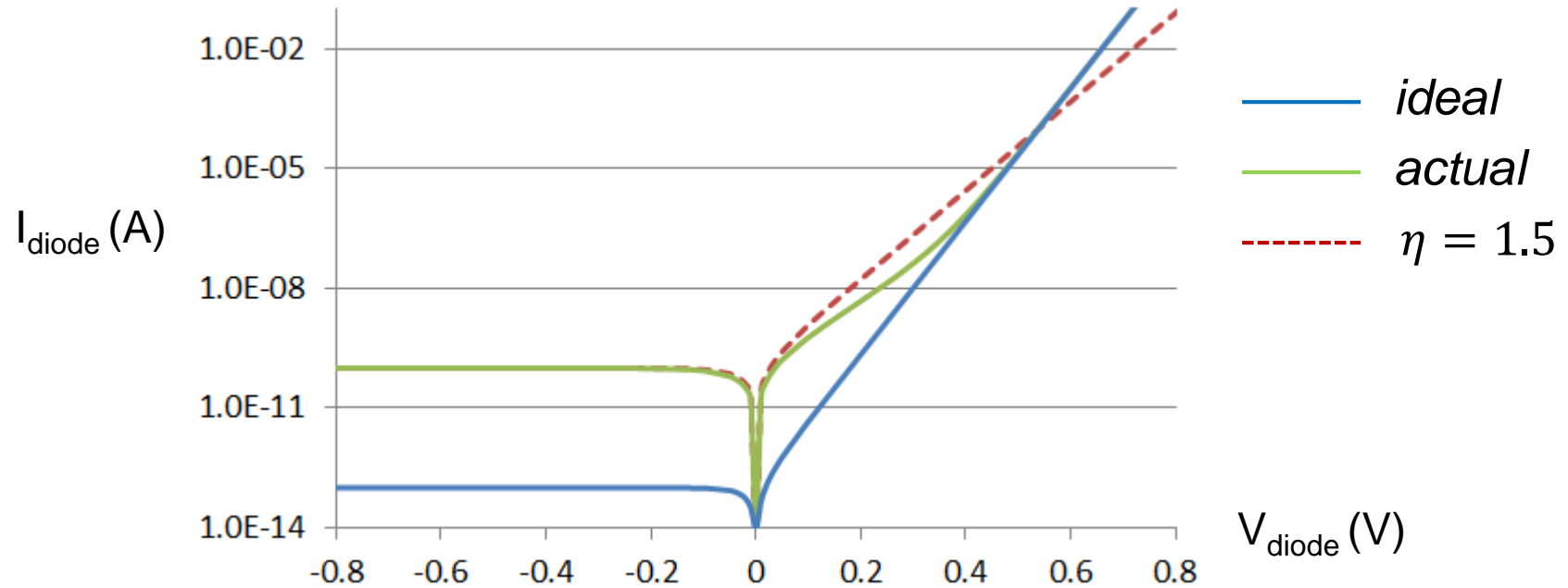
# Generation-Recombination in Depletion Region

- Our analysis assumed that  $J_p$  and  $J_n$  did not change between  $x_p$  and  $x_n$ 
  - There will be extra current due G-R within depletion region
  - Space Charge Region (SCR) or Generation-Recombination current
- Since there are no majority carriers, recombination requires presence of minority holes *and* electrons

$$I_{SCR} = I_{0,SCR} \left( e^{qV/2kT} - 1 \right)$$

- Under forward bias, SCR current increases at only 120mV/decade
- At high forward bias, diffusion current dominates
- Under reverse bias, depletion region is devoid of carriers, so electron-hole pairs will be thermally generated and immediately swept across junction by electric field.
- This significantly increases leakage current ( $I_{0,SCR} \gg I_0$ )

# Non-Ideal Diode Behavior



- Account for this extra current with **ideality factor  $\eta$**

$$I = I_{0,SCR} \left( e^{qV/\eta kT} - 1 \right), \quad 1 < \eta < 2$$

# Example: PN Diode currents

- Consider a PN junction diode at 300° K with the following characteristics:

$$N_a = N_d = 10^{16} \text{ cm}^{-3}$$

$$\tau_{p0} = \tau_{n0} = 5 \times 10^{-7} \text{ s}$$

$$D_n = 25 \text{ cm}^2/\text{s}$$

$$\text{area} = 0.01 \text{ mm}^2$$

$$D_p = 10 \text{ cm}^2/\text{s}$$

- Calculate ideal reverse saturation current
- Calculate current with forward bias of 0.65V
- Calculate electric field in N neutral region with forward bias of 0.65V