

# Maximum Likelihood Synchronization for DVB-T2 in Unknown Fading Channels

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## Introduction

- ✓ We consider the **time delay** and **carrier frequency offset** (CFO) estimation problem for the digital video broadcasting-second generation terrestrial (DVB-T2) signals over an **unknown fading channel**.
- ✓ The **special preamble**, i.e., **P1 symbol**, designed for fast synchronization of the DVB-T2 frames is exploited.
- ✓ Our proposed schemes can jointly estimate the delay and CFO by maximum likelihood (ML) methods.

## Structure of the P1 symbol

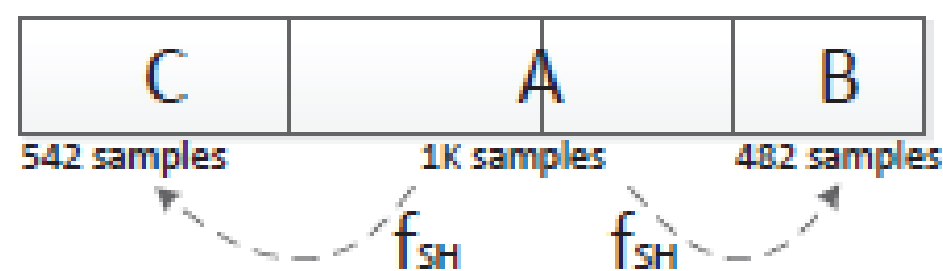


Fig. 1. Time domain structure of the P1 symbol.

Each DVB-T2 frame starts with a P1 symbol of duration 2048 (2K) samples. As shown in Fig. 1, the 2K samples are divided into three parts: A, B, and C.

- ❖ **Part A:** Generated by applying a 1024-point inverse Fourier transform on the signaling vector (similar to the OFDM symbol); only 384 specific sub-carriers are active, while the other sub-carriers carry zero symbols (null carriers).
- ❖ **Part B:** Repeat the last 482 samples of Part A with a frequency shift of  $f_{SH}$ .
- ❖ **Part C:** Repeat the first 542 samples of Part A with a frequency shift of  $f_{SH}$ .

Therefore, the P1 symbol can be formulated as

$$\mathbf{s}_{P1} = \mathbf{E} \mathbf{T} \mathbf{P} \mathbf{d}$$

where  $\mathbf{d}$  is the signaling vector in the frequency domain,  $\mathbf{P}$  is the active carrier pattern matrix,  $\mathbf{T}$  is the inverse Fourier matrix, and  $\mathbf{E}$  is the frequency shift matrix.

## Problem Formulation

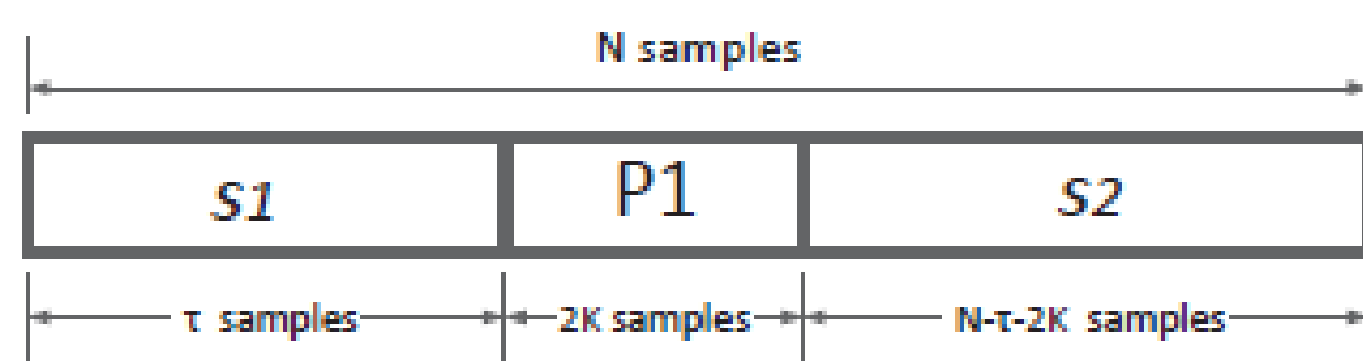


Fig. 2. Transmitted signal during the observing window.

$N$  ( $N > 2048$ ) consecutive samples are collected in a column vector  $\mathbf{x}$  (see Fig. 2) for each estimation procedure, where one P1 symbol is captured.

$$\begin{aligned} \mathbf{x} &= \alpha \mathbf{s} \odot \mathbf{e} + \mathbf{w} \\ \mathbf{s} &= [s(0), s(1), \dots, s(N-1)]^T \\ s(n) &= \begin{cases} s_1(n), & n \in [0, \tau - 1] \\ s_{P1}(n - \tau), & n \in [\tau, \tau + 2N_a - 1] \\ s_2(n - \tau - 2N_a), & n \in [\tau + 2N_a, N - 1] \end{cases} \\ \mathbf{e} &= [1, e^{j2\pi\Phi}, \dots, e^{j2\pi\Phi(N-1)}]^T \\ \mathbf{w} &= [w(0), w(1), \dots, w(N-1)]^T \sim \mathcal{CN}(\mathbf{0}, \eta \mathbf{I}_N) \end{aligned}$$

where  $\alpha$  denotes the unknown coefficient regarding the channel gain,  $\tau$  is the delay in the unit of samples,  $\Phi$  is the normalized CFO, and  $\eta$  is the noise power. **The problem of interest is to jointly estimate the time delay and CFO from the observations  $\mathbf{x}$  by means of ML methods.**

## Proposed Approaches

1. Model the transmitted signal  $\mathbf{s}$  as **zero-mean complex Gaussian distributed** (Central Limit Theorem).

$$\begin{aligned} \mathbf{x} &\sim \mathcal{CN}(\mathbf{0}, \mathbf{R}_x) \\ \mathbf{R}_x &= \mathbf{K}(\Phi) \mathbf{Q} \mathbf{K}(\Phi)^H \\ [\mathbf{K}(\Phi)]_{p,p} &= e^{j2\pi\Phi(p-1)} \text{ for } p = 1, 2, \dots, N \\ \mathbf{Q} &= \eta_s \mathbf{R}_s(\tau) + \eta \mathbf{I}_N \\ \mathbf{R}_s(\tau) &= \begin{bmatrix} \mathbf{I}_\tau & \mathbf{0}_{\tau \times 2N_a} & \mathbf{0}_{\tau \times N'} \\ \mathbf{0}_{2N_a \times \tau} & \mathbf{R} & \mathbf{0}_{2N_a \times N'} \\ \mathbf{0}_{N' \times \tau} & \mathbf{0}_{N' \times 2N_a} & \mathbf{I}_{N'} \end{bmatrix} \\ \mathbf{R} &= E\{\mathbf{s}_{P1} \mathbf{s}_{P1}^H\} = \mathbf{E} \mathbf{T} \mathbf{P} \mathbf{P}^H \mathbf{T}^H \mathbf{E}^H \end{aligned}$$

$$\begin{aligned} \Lambda(\eta_s, \tau, \Phi) &= -\frac{\Gamma_2(\tau)}{\eta_s + \eta} - (N - 2N_a) \ln(\eta_s + \eta) - N \ln \pi \\ &\quad - \mathbf{x}_{P1}(\tau)^H \mathbf{K}_{P1}(\tau, \Phi) \mathbf{B}^{-1} \mathbf{K}_{P1}(\tau, \Phi)^H \mathbf{x}_{P1}(\tau) \\ &\quad - \ln |\mathbf{B}|, \\ (\hat{\eta}_s(\tau), \hat{\Phi}(\tau)) &= \arg \max_{\eta_s, \Phi} \Lambda(\eta_s, \Phi | \tau) \\ \hat{\tau} &= \arg \max_{\tau} \Lambda(\hat{\eta}_s(\tau), \tau, \hat{\Phi}(\tau)) \\ \hat{\eta}_s &= \hat{\eta}_s(\hat{\tau}) \text{ and } \hat{\Phi} = \hat{\Phi}(\hat{\tau}) \end{aligned}$$

2. Model the transmitted signal  $\mathbf{s}$  as **deterministic but unknown**.

$$\begin{aligned} \mathbf{x} &= \mathbf{s} \odot \mathbf{e} + \mathbf{w} = \mathbf{K}(\Phi) \mathbf{s} + \mathbf{w} \\ \mathbf{x} &\sim \mathcal{CN}(\mathbf{K}(\Phi) \mathbf{s}, \eta \mathbf{I}_N) \end{aligned}$$

DISTRIBUTION

DML

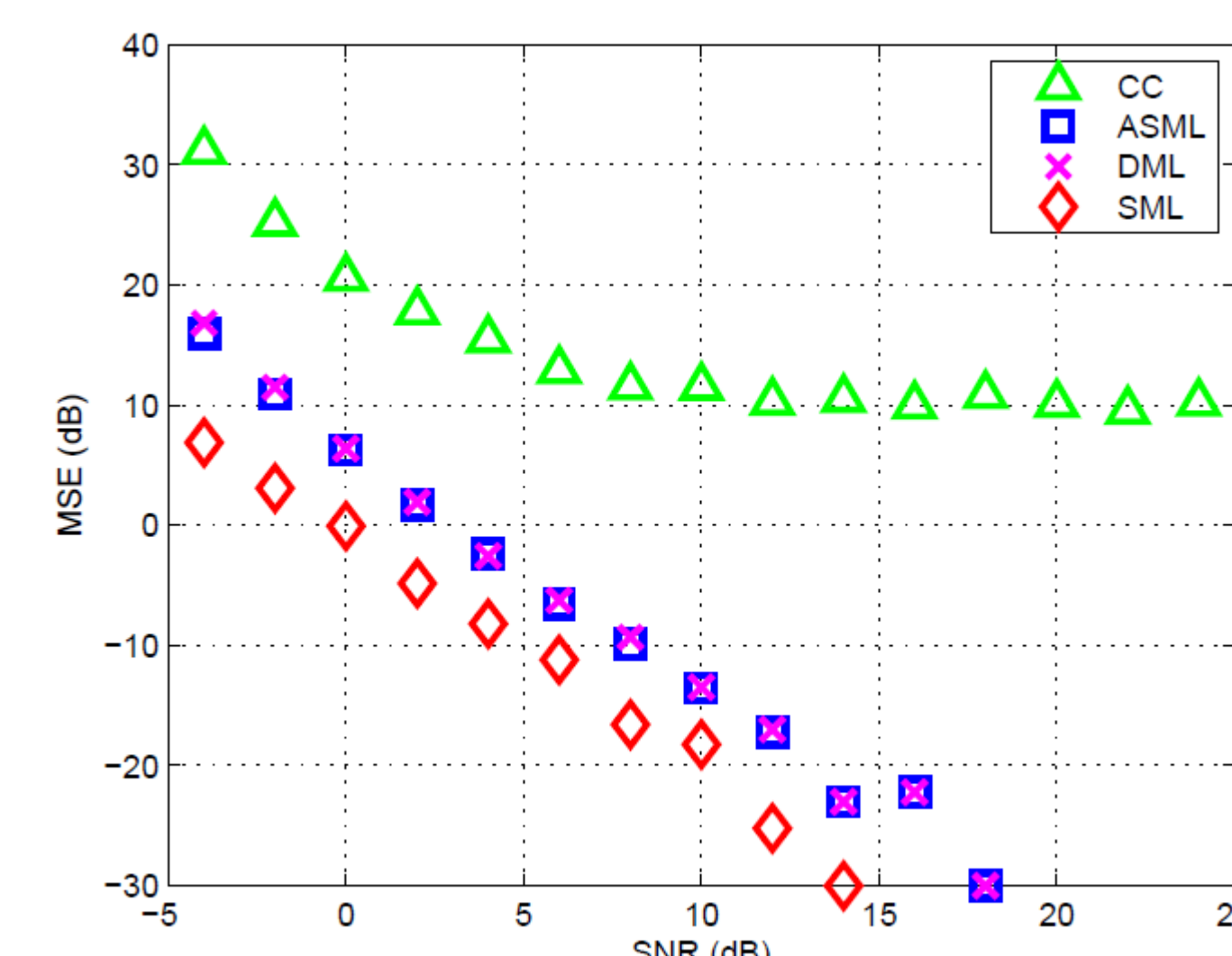
$$\begin{aligned} \Lambda(\mathbf{s}, \tau, \Phi, \eta) &\triangleq \ln f(\mathbf{x} | \mathbf{s}, \tau, \Phi, \eta) \\ &= -\frac{\Delta}{\eta} - N \ln \eta - N \ln \pi \\ (\hat{\mathbf{s}}, \hat{\tau}, \hat{\Phi}, \hat{\eta}) &= \arg \max_{\mathbf{s}, \tau, \Phi, \eta} \Lambda(\mathbf{s}, \tau, \Phi, \eta) \\ (\hat{\mathbf{s}}, \hat{\tau}, \hat{\Phi}) &= \arg \min_{\mathbf{s}, \tau, \Phi} \Delta(\mathbf{s}, \tau, \Phi) \\ \hat{\eta} &= \frac{\Delta(\hat{\mathbf{s}}, \hat{\tau}, \hat{\Phi})}{N} \end{aligned}$$

MAX LLF

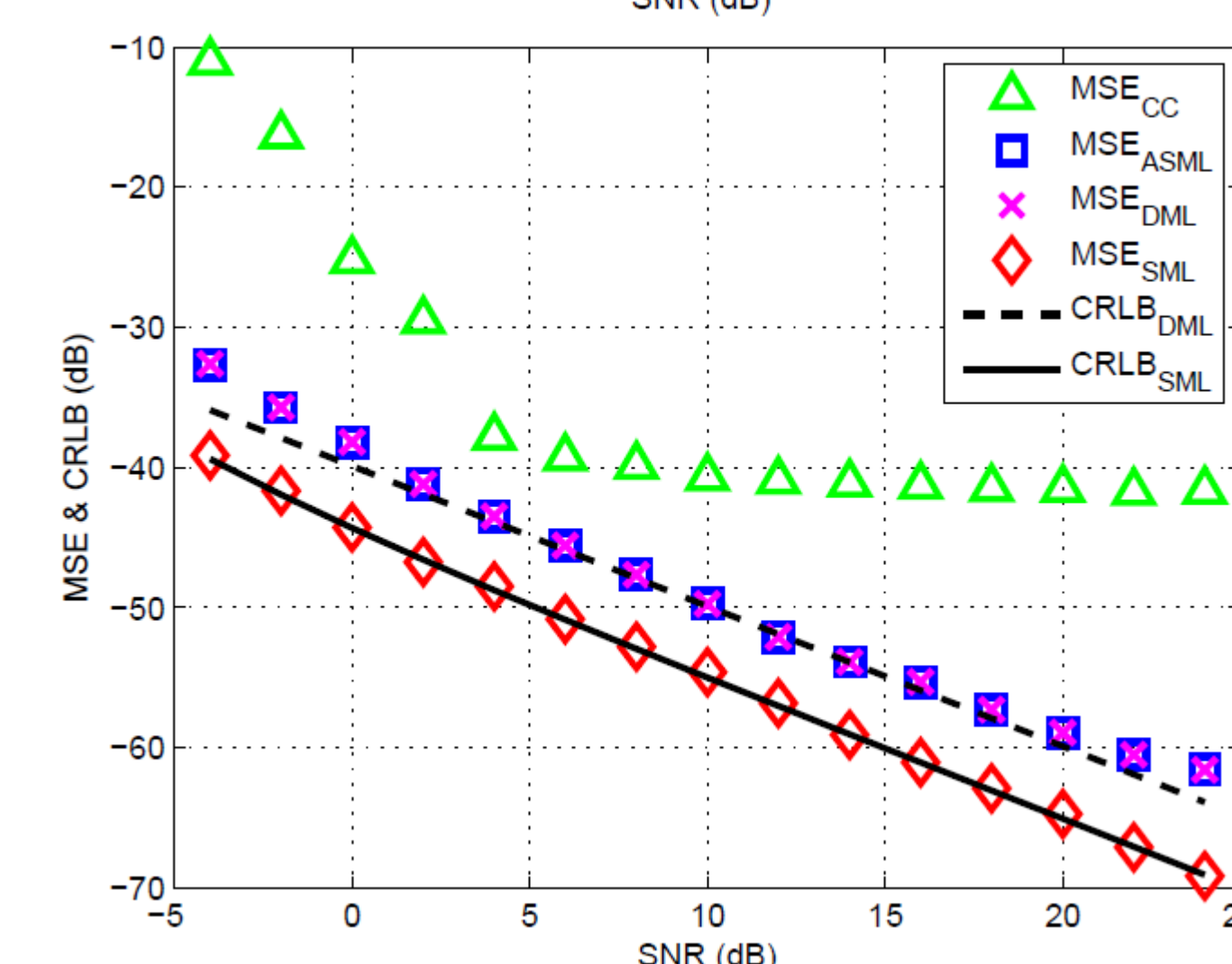
## Simulation Results

$N = 6N_a$	$M$	$\phi$	$\Phi$	$\tau$	$\eta$
6144	384	0.45	$\frac{0.45}{1024}$	100	1

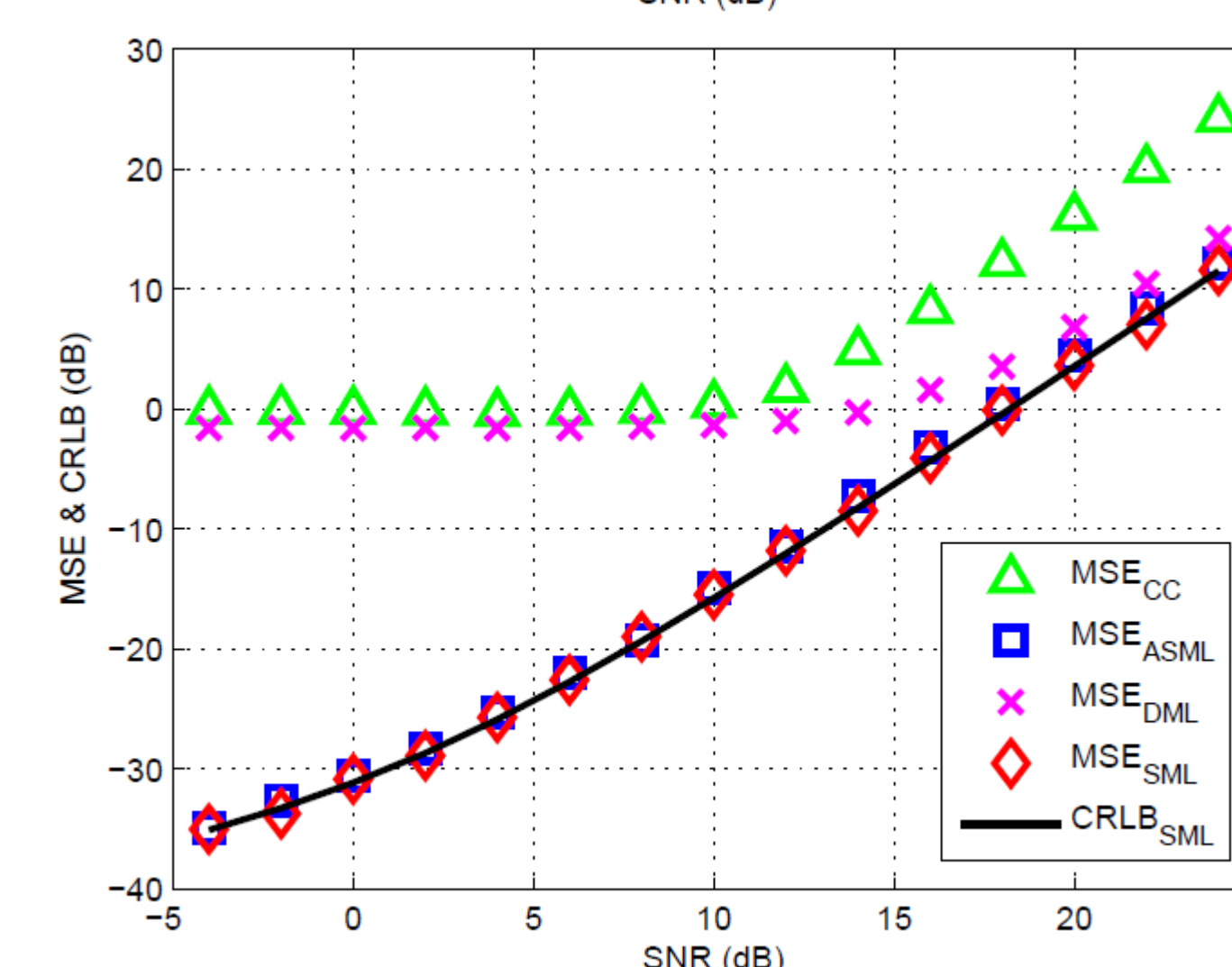
Delay



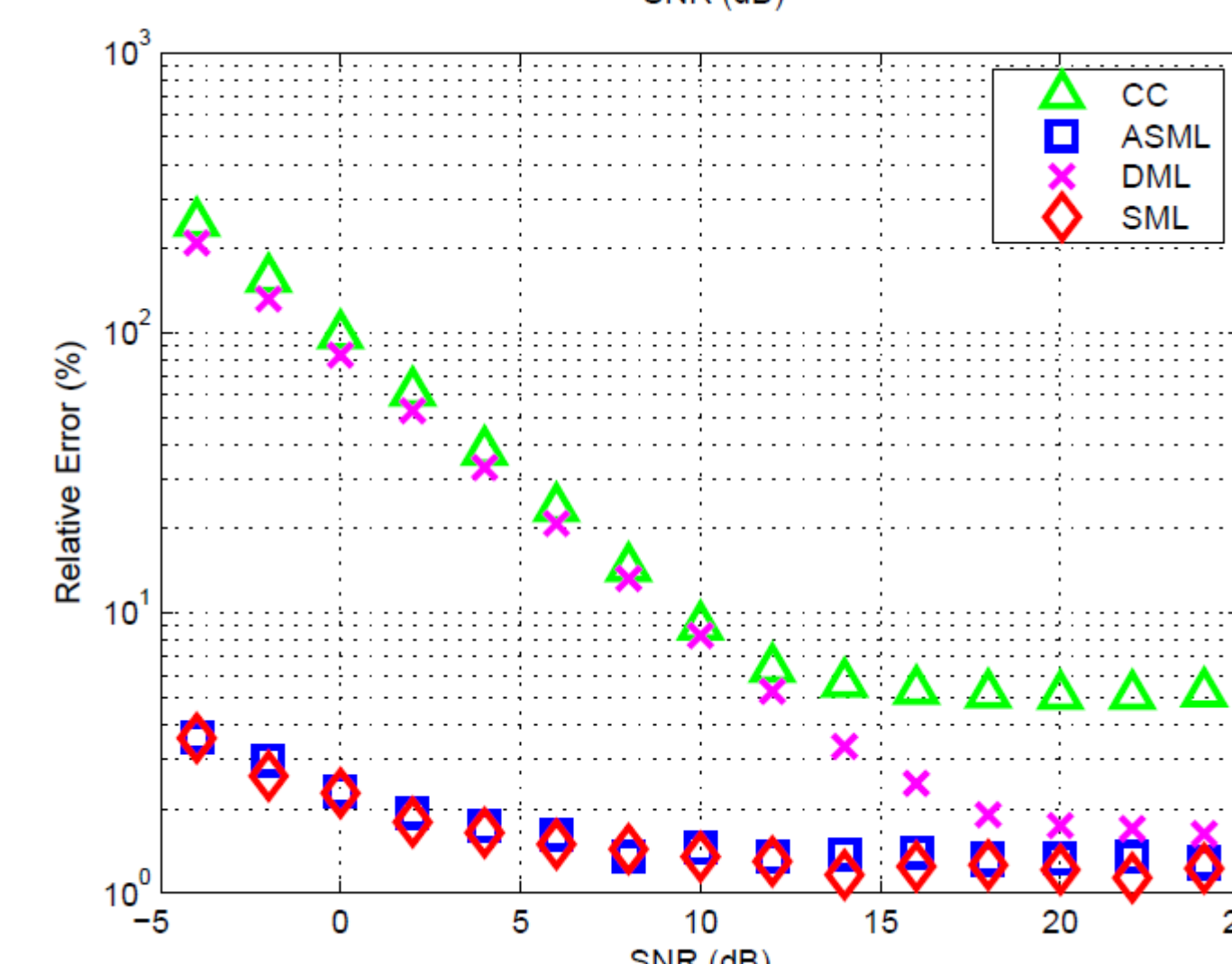
CFO



s Power



s Power



## Conclusion

- ❖ Unlike previous studies, we consider a more general channel environment where the channel coefficient is unknown.
- ❖ **Stochastic Model** => SML, ASML.
- ❖ **Unknown Deterministic Model** => DML.
- ❖ **CRLB** = SML  $\geq$  ASML  $\geq$  DML  $>$  CC.
- ❖ DML is more flexible and has a lower complexity.