

**Ma 227**

**Exam III B**

**4/25/05**

Name: \_\_\_\_\_

Lecture Section: \_\_\_\_\_ Lecturer: \_\_\_\_\_

*I pledge my honor that I have abided by the Stevens Honor System.* \_\_\_\_\_

**You may not use a calculator, cell phone, or computer while taking this exam. All work must be shown to obtain full credit. Credit will not be given for work not reasonably supported. When you finish, be sure to sign the pledge.**

Score on Problem #1 \_\_\_\_\_

#2 \_\_\_\_\_

#3 \_\_\_\_\_

Total Score \_\_\_\_\_

**1a [15 pts.]** Evaluate the line integral  $\int_C \vec{F} \cdot d\vec{r}$ , if

$$\vec{F}(x,y) = yz\vec{i} - xz\vec{k}$$

where  $C$  is the plane path  $x(t) = 2t - 1, y(t) = 2 - 4t, z(t) = t, 0 \leq t \leq 1$ .

**1b [15 pts.]** Let  $\vec{r} = x\vec{i} + y\vec{j} + z\vec{k}$  and  $r = |\vec{r}|$ . Show that

$$\nabla(\ln r) = \frac{\vec{r}}{r^2}$$

**2a [20 pts.]** Find a function  $\Phi(x, y, z)$  such that  $\nabla\Phi = \vec{F}$ , where

$$\vec{F}(x, y, z) = (3x^2 + z)\vec{i} + (3y^2 - z)\vec{j} + (3z^2 - y + x)\vec{k}$$

**2b [20 pts.]** Verify that Green's Theorem is true for the line integral

$$\oint_C x^2y dx + xy^2 dy$$

where  $C$  is the triangle with vertices  $(0,0)$ ,  $(1,0)$ ,  $(1,3)$ . Sketch the triangle.

**3 a [10 pts.]** Let  $S$  be the portion of the cylinder  $x^2 + y^2 = 9$  that lies between  $z = 0$  and  $z = 4$ . Use cylindrical coordinates to give a parametrization of  $S$ .

**3 b [20 pts.]** Give an expression for

$$\iint_S xz dS$$

where  $S$  is the surface in part 3a. Do *not* evaluate your expression.