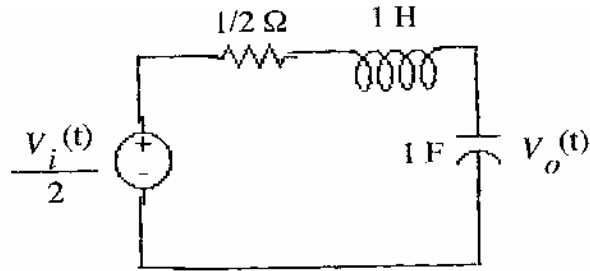


**16.**

**a.** Writing the node equations,  $\frac{V_o - V_i}{s} + \frac{V_o}{s} + V_o = 0$ . Solve for  $\frac{V_o}{V_i} = \frac{1}{s+2}$ .

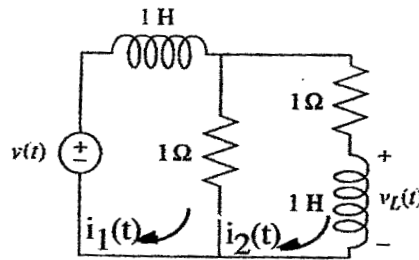
b. Thevenizing,



Using voltage division,  $V_o(s) = \frac{V_i(s)}{2} \frac{\frac{1}{s}}{\frac{1}{2} + s + \frac{1}{s}}$ . Thus,  $\frac{V_o(s)}{V_i(s)} = \frac{1}{2s^2 + s + 2}$

17.

a.



Writing mesh equations

$$(s+1)I_1(s) - I_2(s) = V_i(s)$$

$$-I_1(s) + (s+2)I_2(s) = 0$$

But,  $I_1(s) = (s+2)I_2(s)$ . Substituting this in the first equation yields,

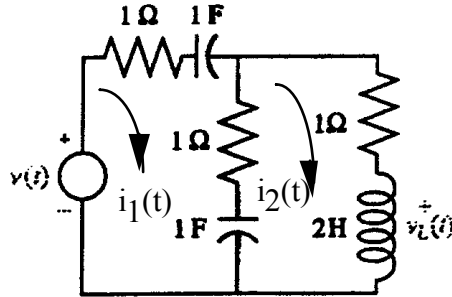
$$(s+1)(s+2)I_2(s) - I_2(s) = V_i(s)$$

or

$$I_2(s)/V_i(s) = 1/(s^2 + 3s + 1)$$

But,  $V_L(s) = sI_2(s)$ . Therefore,  $V_L(s)/V_i(s) = s/(s^2 + 3s + 1)$ .

b.



$$\left(2 + \frac{2}{s}\right)I_1(s) - \left(1 + \frac{1}{s}\right)I_2(s) = V(s)$$

$$-\left(1 + \frac{1}{s}\right)I_1(s) + \left(2 + \frac{1}{s} + 2s\right)I_2(s) = 0$$

Solving for  $I_2(s)$ :

$$I_2(s) = \frac{\begin{vmatrix} \frac{2(s+1)}{s} & V(s) \\ -\frac{s+1}{s} & 0 \end{vmatrix}}{\begin{vmatrix} \frac{2(s+1)}{s} & -\frac{s+1}{s} \\ -\frac{s+1}{s} & \frac{2s^2 + 2s + 1}{s} \end{vmatrix}} = \frac{V(s)s}{4s^2 + 3s + 1}$$

$$\text{Therefore, } \frac{V_L(s)}{V(s)} = 2s \frac{I_2(s)}{V(s)} = \frac{2s^2}{4s^2 + 3s + 1}$$

23.

Writing the equations of motion, where  $x_2(t)$  is the displacement of the right member of springr,

$$(s^2+s+1)X_1(s) -X_2(s) = 0$$

$$-X_1(s) +X_2(s) = F(s)$$

Adding the equations,

$$(s^2+s)X_1(s) = F(s)$$

From which,  $\frac{X_1(s)}{F(s)} = \frac{1}{s(s+1)}$ .

26.

$$(s^2 + 3s + 2) X_1(s) - (s + 1) X_2(s) = 0$$

$$-(s + 1) X_1(s) + (s^2 + 2s + 1) X_2(s) = F(s)$$

Solving for  $X_1(s)$ ;  $X_1 = \frac{\begin{vmatrix} 0 & -(s+1) \\ F & s^2+2s+1 \end{vmatrix}}{\begin{vmatrix} s^2+3s+2 & -(s+1) \\ -(s+1) & s^2+2s+1 \end{vmatrix}} = \frac{F(s)}{s^3+4s^2+4s+1}$ . Thus,  $\frac{X_1}{F(s)} = \frac{1}{s^3+4s^2+4s+1}$

27.